

Самозахват мощных лазерных импульсов и ядерная фотоника

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XIX НАУЧНАЯ ШКОЛА
“Нелинейные волны -2020”

29 февраля - 6 марта 2020 г.

Contributors

recent (2018-2020) advances in relativistic nonlinear optics for applications

Lebedev Physics Institute & CFAR, VNIIA, ROSATOM, Russia :

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Weizmann Institute of Science, Israel :

I.A. Andriyash, V. Malka

Outline

I. Relativistic intense soliton in the service of nuclear photonics:

- **Acceleration of electrons from low-density targets**
 $n_e \sim < n_c$ for maximization of total electron charge.
- **Self-trapping regime. The matched beam spot size to density condition. Laser bullet (soliton).**
- **Production of gammas and pairs. Deep gamma-radiography.**
- **Production of neutrons and photonuclear elementary particles.**
- **Isotope production**

II. New laser-based THz-sources:

- **Ultrafast target charging by laser-accelerated electrons.**
- **THz surface wave.**

III. How to measure relativistic intense laser pulse:

Historical excursion

VOLUME 13, NUMBER 15

PHYSICAL REVIEW LETTERS

12 OCTOBER 1964

SELF-TRAPPING OF OPTICAL BEAMS*

R. Y. Chiao, E. Garmire, and C. H. Townes
Massachusetts Institute of Technology, Cambridge, Massachusetts
(Received 1 September 1964)

$$R=f(I, n_{\text{eff}})$$

Kerr effects

Molecular orientation, electrostriction, electronic polarizability

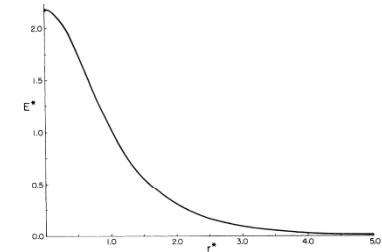


FIG. 1. Calculated radial distribution of the electric field in a self-trapped electromagnetic wave.

SOVIET PHYSICS JETP

VOLUME 23, NUMBER 6

DECEMBER 1966

*SELF-FOCUSING AND SELF-TRAPPING OF INTENSE LIGHT BEAMS IN A
NONLINEAR MEDIUM*

S. A. AKHMANOV, A. P. SUKHORUKOV, and R. V. KHOKHLOV

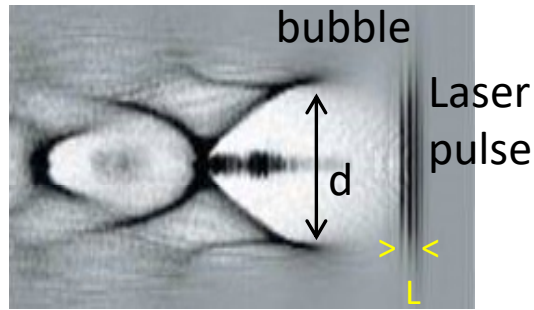
Moscow State University

Submitted to JETP editor December 14, 1965

J. Exptl. Theoret. Phys. (U.S.S.R.) 50, 1537-1549 (June, 1966)

beams become self-trapped in a medium with $n_2 > 0$ and $n_4 < 0$. The diameter of such a self-trapped beam oscillates;

Wakefield acceleration of electrons



$0.004n_c$

Tajima T. and Dawson J. M. 1979 Phys. Rev. Lett. **43** 267

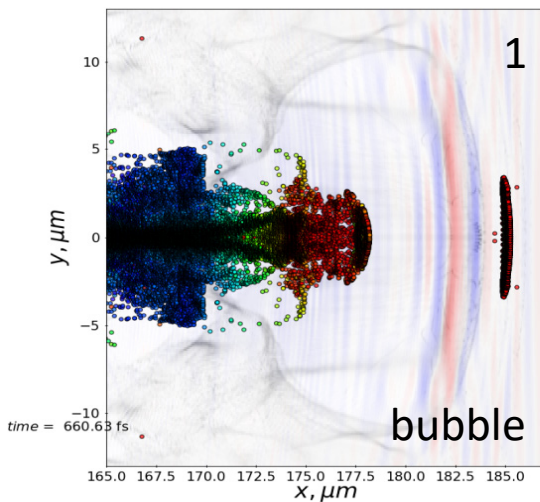
3D plasma wave

Pukhov A. and Meyer-ter-Vehn J., 2002 Appl. Phys. B: Lasers Opt. **74** 355

"bubble" regime

$$L < \lambda_p \quad L < d$$

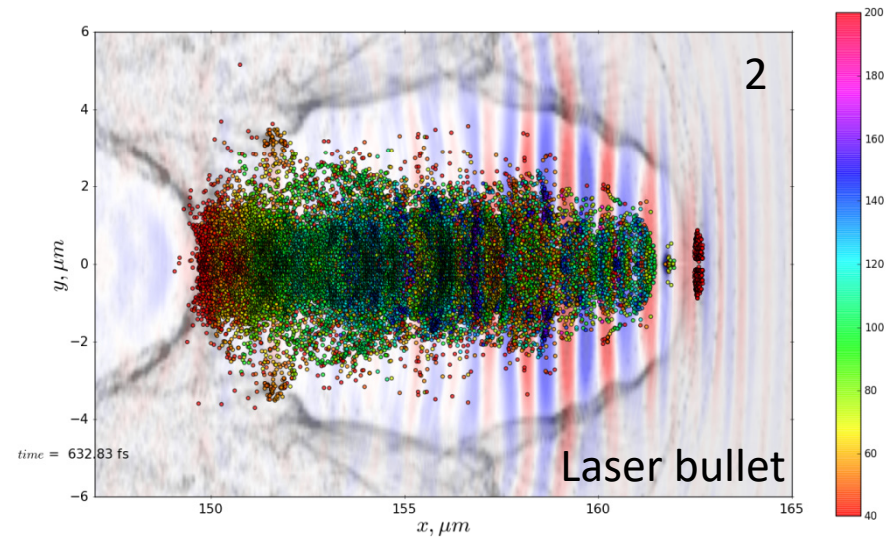
Quasi-monoenergetic electrons, pC charge
Up to 3 GeV (gas jet) and 4.2 GeV (capillary)



~~$L < \lambda_p \quad L < d$~~



$$L > \lambda_p, L > d$$

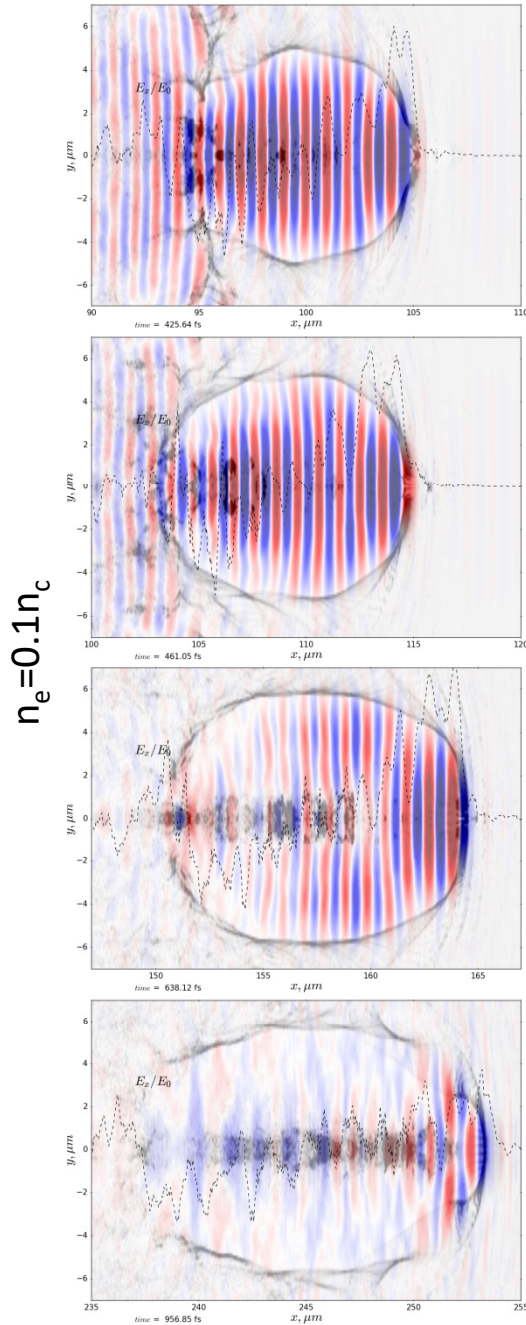


$a_0 = 10, R = 10\lambda, \tau = 13\text{fs}, n_e = 0.04n_c$

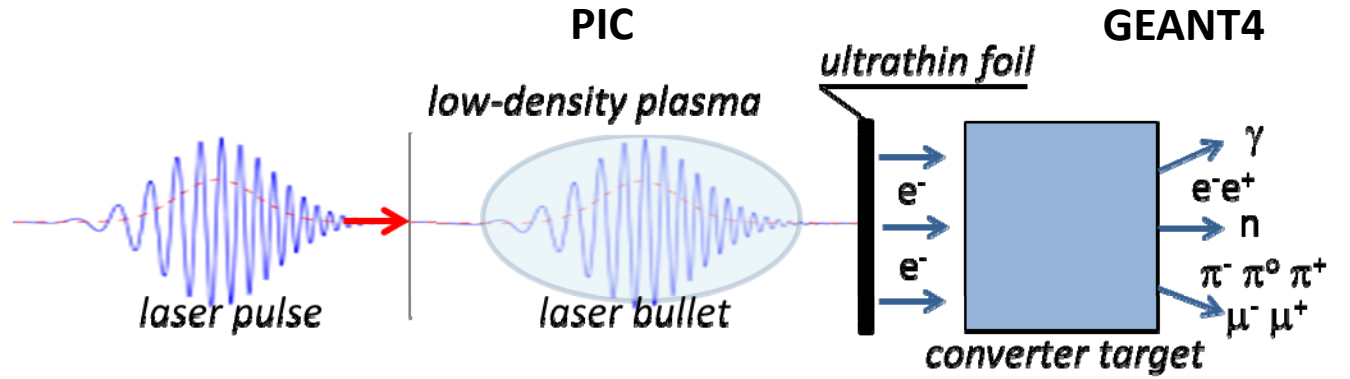
$$E_1/E_2 \approx 2$$

$a_0 = 24, R = 2\lambda, \tau = 30\text{fs}, n_e = 0.1n_c$

Laser light self-trapping regime



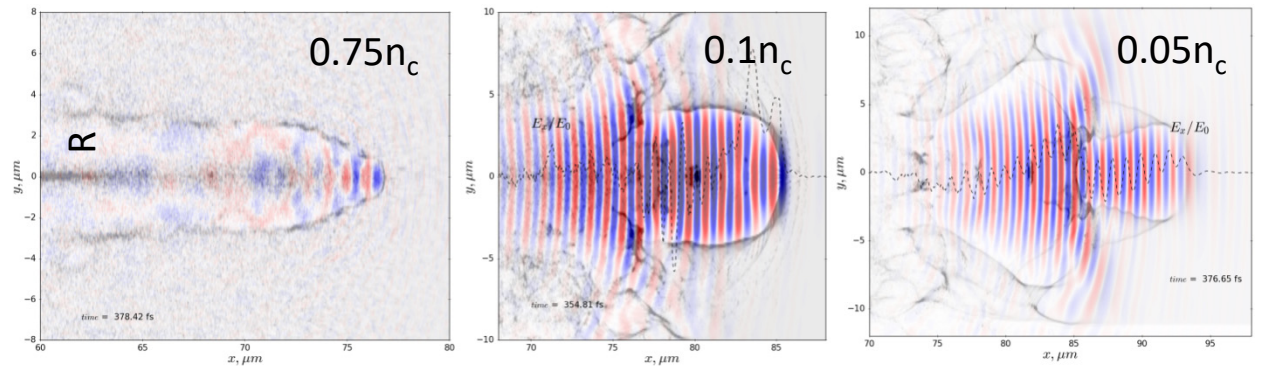
Propagation over ~ 10 Rayleigh lengths



$$R \cong \frac{c}{\omega_p} \alpha \sqrt{a_0}$$

$$a_0 = 0.85 \lambda [\mu\text{m}] \sqrt{I [W/cm^2]} \times 10^{-9} \quad \alpha - \text{numeric factor} \sim (1-2)$$

$$a_0 = 24, R_L = 2\lambda, \tau = 30\text{fs}, P = 100 \text{ TW}$$



R (n, I) - matching

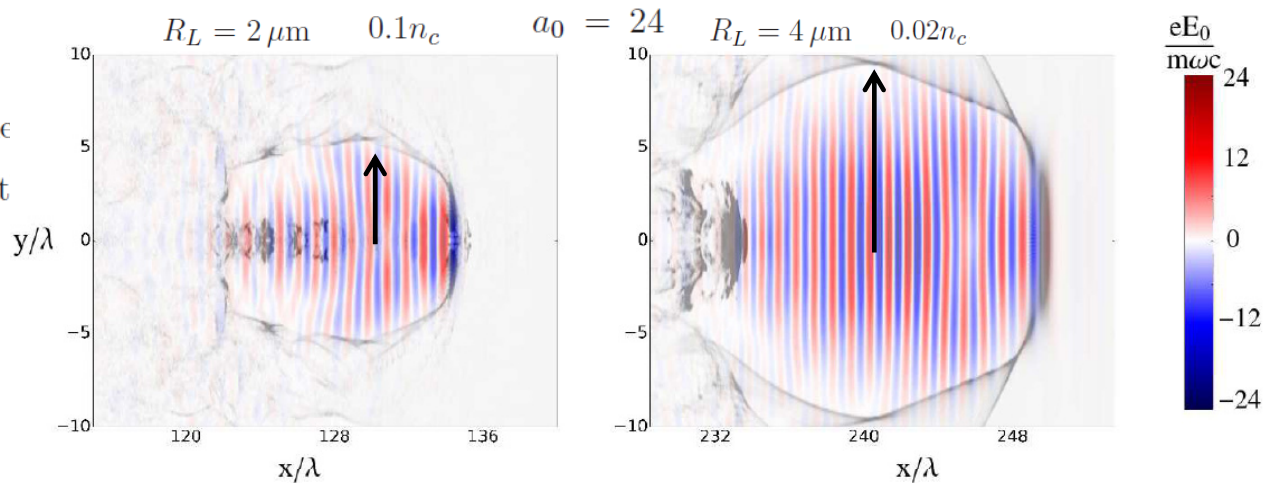
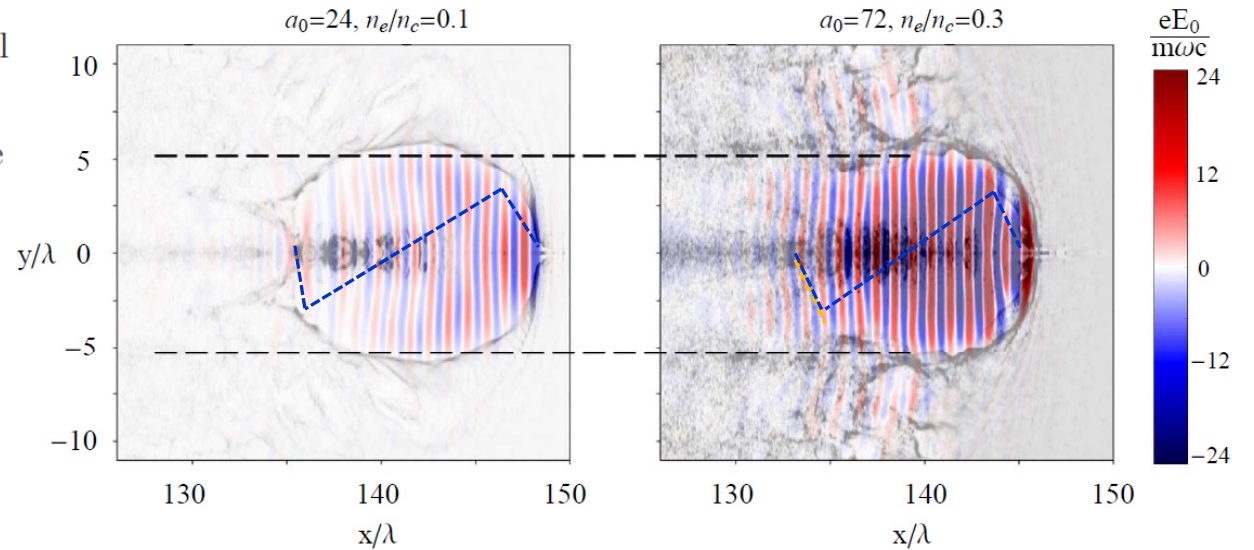
Matching condition \equiv relativistic ($a \gg 1$) self-trapping

Comparison of two self-trapping pulses with initial radius $R_L = 2 \mu\text{m}$ and amplitudes $a_0 = 24$ (left) and $a_0 = 72$ (right) propagating in plasmas with the corresponding electron densities $0.1n_c$ and $0.3n_c$

Laser pulse = soliton

$$\frac{R_1}{R_2} = \sqrt{\frac{a_1 n_2}{a_2 n_1}}$$

Comparison of two self-trapping pulses with the amplitude $a_0 = 24$ and initial radii $R_L = 2 \mu\text{m}$ (left) and $R_L = 4 \mu\text{m}$ (right) propagating in plasmas with the corresponding electron densities $0.1n_c$ and $0.02n_c$



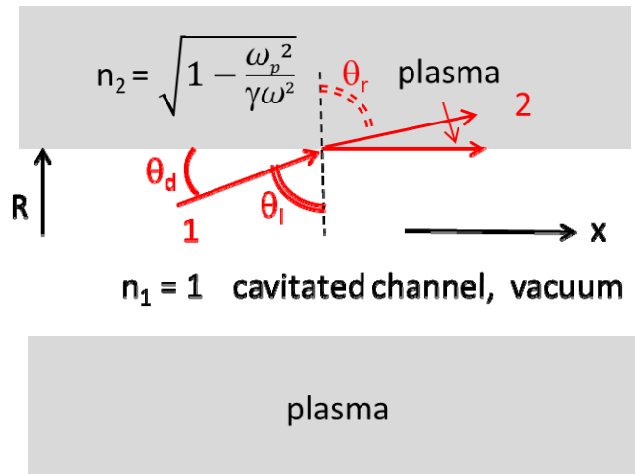
**M.G.Lobok, A.V.Brantov, V.F.Kovalev,
and V.Yu.Bychenkov**

Plasma Phys. Contr. Fus. 61, 124004 (2019)

Physics of the matched cavern spot size condition

$$R \cong \frac{c}{\omega_p} \alpha \sqrt{a_0} \quad R = \frac{c}{\omega} \sqrt{\frac{n_c}{n_e}} \left(\frac{16\alpha^4 P}{P_c} \right)^{1/6} \quad P - \text{laser pulse power}$$

- 1 Gordienko S and Pukhov A 2005 *Phys. Plasmas* 12, 043109 $\alpha \approx 1.12$
- 2 Lu M *et al* 2007 *Phys. Rev. STAB* 10, 061301 $\alpha \approx 2$
- 3 Lobok M G Brantov A V Gozhev D A and Bychenkov V Yu 2018 *Plasma Phys. Control. Fusion* 60 084010 $\alpha \approx 2$



Snell's law

$$\theta_d \simeq \lambda / \pi R \quad \theta_i = \pi/2 - \theta_d$$

$$n_1 \sin \theta_i = n_2 \sin \theta_r$$

condition of the total internal reflection, $\theta_r = \pi/2$

$$\theta_d^2 \simeq \left(\frac{2c}{\omega R} \right)^2 \simeq \frac{\omega_p^2}{\gamma \omega^2} \simeq \frac{\sqrt{2} \omega_p^2}{a_0 \omega^2} \quad \gamma = \sqrt{1 + a_0^2/2} \simeq a_0 / \sqrt{2}$$

$$\rightarrow R \cong \frac{c}{\omega_p} 2^{3/4} \sqrt{a_0}$$

Laser beam self-trapping: plane geometry

NLSE + relativistic nonlinearity of electron mass

$$2ik\partial_z E + \partial_{xx} E + k^2 \frac{\epsilon_{nl}}{\epsilon_0} E = 0, \quad E = A \exp\left(i \frac{\nu z}{2kd^2}\right), \quad \gamma = \sqrt{1 + |E/E_{rel}|^2}, \quad \mathbf{E} = \mathbf{E}(x, z, t - z\sqrt{\epsilon_0}/c),$$

$$\epsilon_0 = 1 - \frac{4\pi e^2 n_{e0}}{(m_0 \omega^2)}, \quad \epsilon_{nl} = \epsilon_0 \frac{k_p^2}{k^2} \left(1 - \frac{1}{\gamma}\right), \quad k_p^2 = \frac{4\pi e^2 n_{e0}}{m_0 c^2}, \quad k = \frac{\omega}{c} \sqrt{\epsilon_0}, \quad E_{rel}^2 = \left(\frac{\omega c m_0}{e}\right)^2.$$

In dimensionless variables $z/2kd^2$, x/d , A/A_0 , the solution depends upon two parameters:

$$\rho = \omega_{pe} d / c \text{ and } i_0 = (e/\omega m_0 c)^2 A_0^2 = I_0 / I_r, \text{ with } I_0 = (c/4\pi) A_0^2, \quad I_r = \omega^2 m_0^2 c^3 / (4\pi e^2).$$

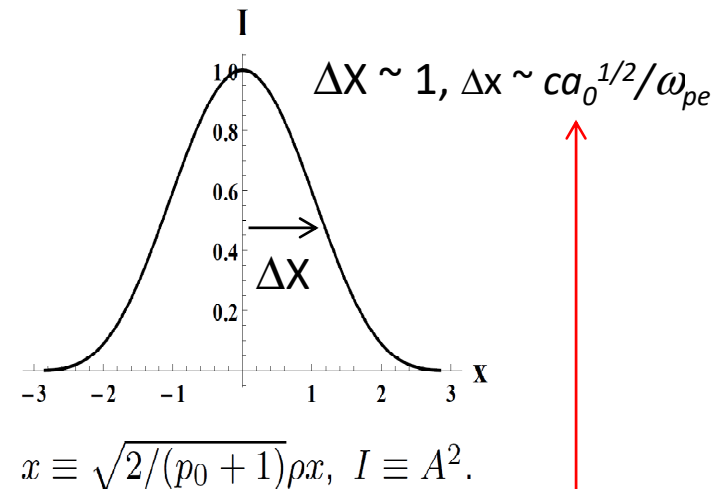
Self-trapping solution for $\nu = \rho^2(1 + (2/i_0)(1 - p_0))$

$$\sqrt{\frac{2}{(p_0 + 1)}} \rho x = -\pi + 2 \arctan \sqrt{\frac{p + 1}{p_0 - p}} - \sqrt{\frac{2}{p_0 - 1}} \ln \frac{2\sqrt{p_0 - p} + \sqrt{2(p_0 - 1)(p + 1)}}{\sqrt{2(p_0 + 1)(p - 1)}},$$

$$p_0 = \sqrt{1 + i_0}, \quad p = \sqrt{1 + i_0 A^2},$$

Limiting case $i_0 \rightarrow 0$: $A^2 = \cosh^{-2}(x\rho\sqrt{i_0}/2)$.

$$\Delta x \omega_{pe} \sim \frac{m_e}{a_0} \rightarrow \frac{\Delta x}{\sqrt{m_e}} \sim \frac{m_e}{a_0} \rightarrow \Delta x \sim \frac{(m_e)^{3/2}}{a_0} \sim a_0^{1/2}$$



Analytical theory of relativistic self-focusing

$$2ik\partial_z E + \Delta_{\perp} E + k^2(\epsilon_{nl}/\epsilon_0)E = 0, \quad E(0, \mathbf{r}) = E_0(\mathbf{r})$$

$$\epsilon_{nl} = \epsilon_0 \frac{k_p^2}{k^2} \left(1 - \frac{n_e}{\gamma n_{e0}} \right)$$

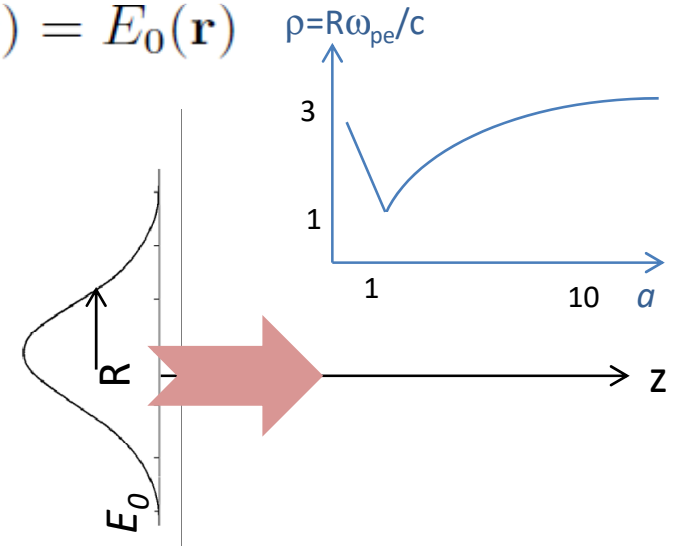
$$\gamma = \sqrt{1 + |E/E_{rel}|^2}$$

$$E_{rel}^2 = (\omega c m_0 / e)^2$$

$$N_e = \frac{(1 + k_p^{-2} \Delta_{\perp} \gamma)}{(1 - \exp(-\alpha_0 (1 + k_p^{-2} \Delta_{\perp} \gamma)))}$$

$$n_e = n_{e0} N_e(\gamma)$$

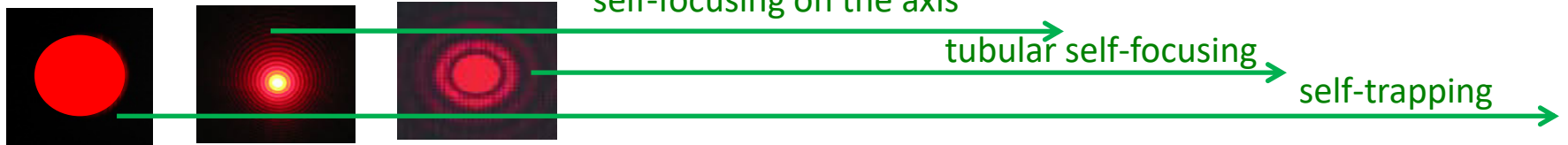
relativistic electron mass + and ponderomotive charge-displacement



V.F.Kovalev & V.Yu.Bychenkov
Phys. Rev. E **99**, 043201 (2019)

Gaussian radial intensity distribution at the plasma boundary

- Search for new regimes of relativistic self-focusing



- Finding of window parameters for different regimes of channeling

three stationary self-focused waveguide propagation modes

Self-trapping: $R\omega_p/c = F(a_0), a_0 \gg 1 \rightarrow R\omega_p/c \sim \sqrt{a_0}$

- balance of forces
- no filamentation

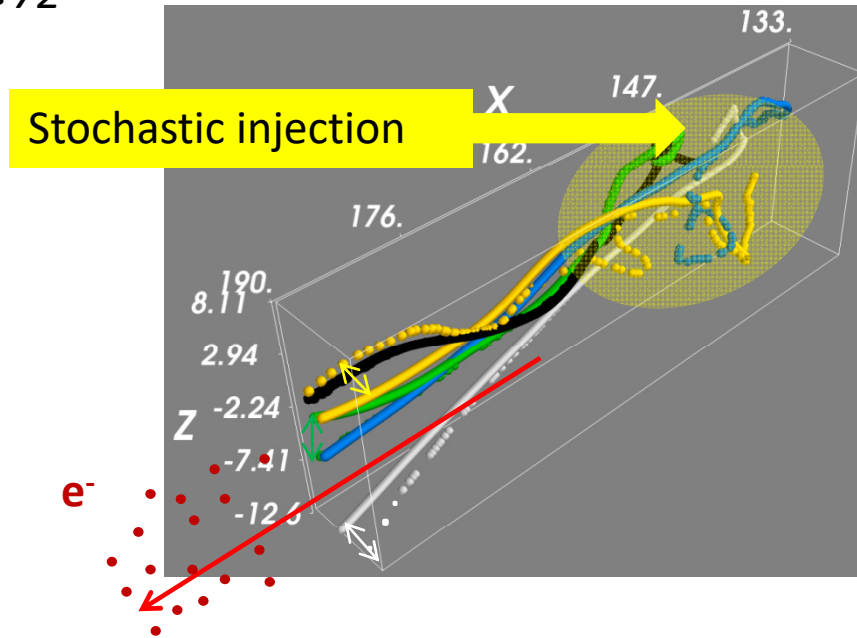
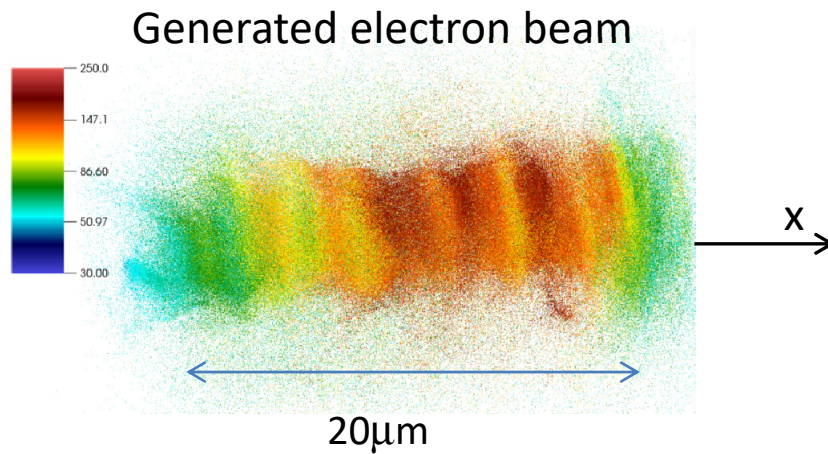
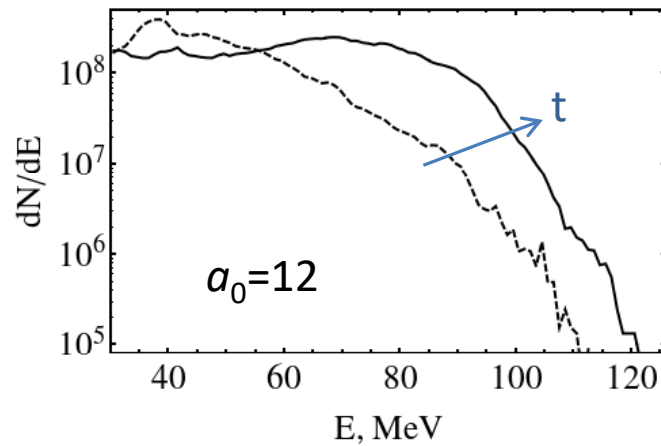
Electron acceleration. Stochastic injection.

Etching rate → optimum target thickness:
C.D.Decker *et al.*, Phys. Plasmas **3**, 2047 (1996)

$$L_{\text{dep}} = L_{\text{etch}} \approx c\tau(n_c/4n_e)a_0$$

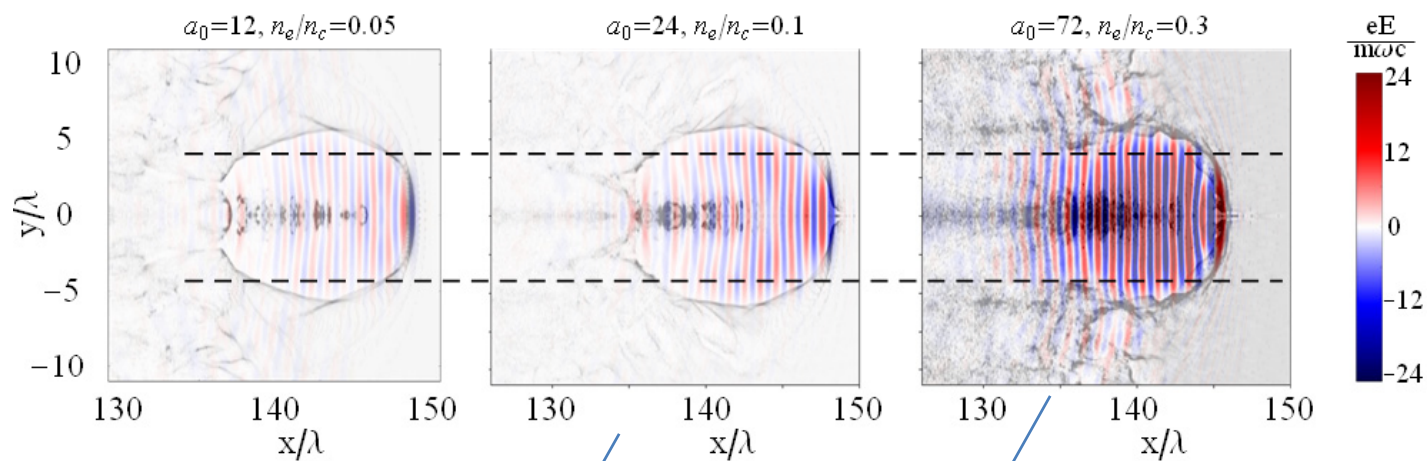
High conversion
to MeV electrons
($E > 30$ MeV) 15 %!

$$a_0 = 12 \div 72$$

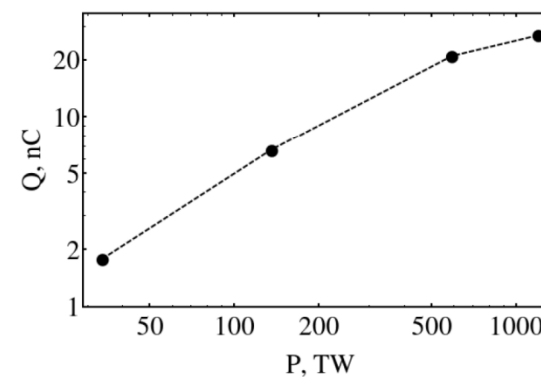
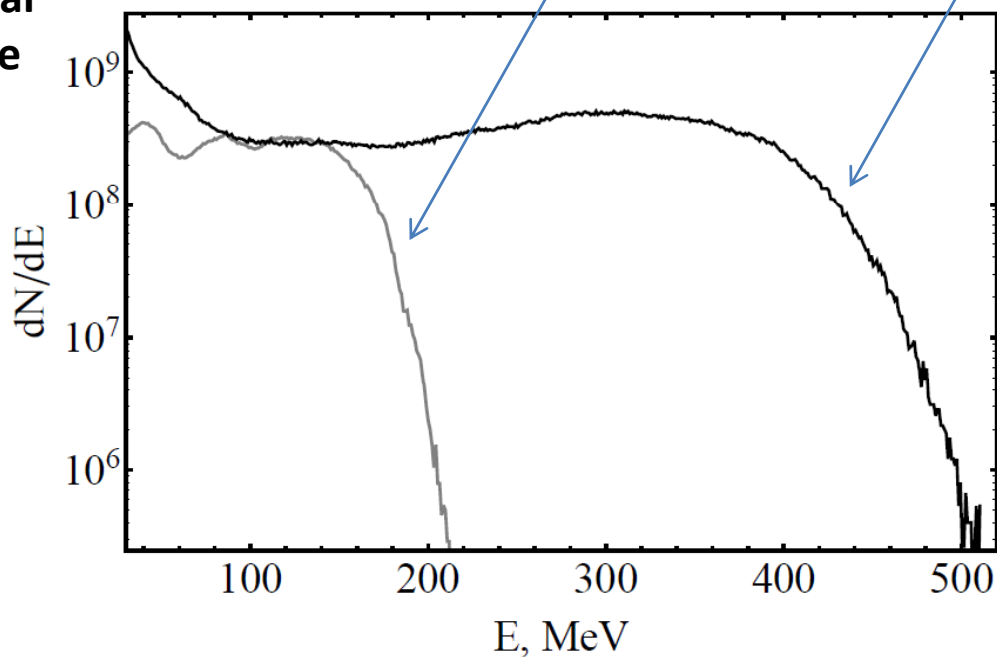


M.G.Lobok, A.V.Brantov, D.A.Gozhev,
and V.Yu.Bychenkov
Plasma Phys. Contr. Fus. **60**, 084010 (2018)

Intensity dependence

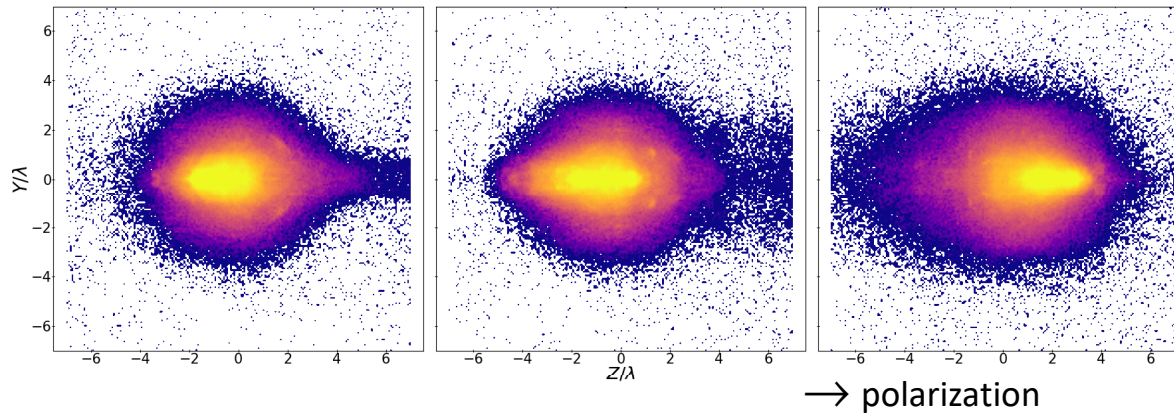


Very universal
plateau-type
spectra



Dependence of the maximum total electron charge on the laser power for a 30 fs pulse

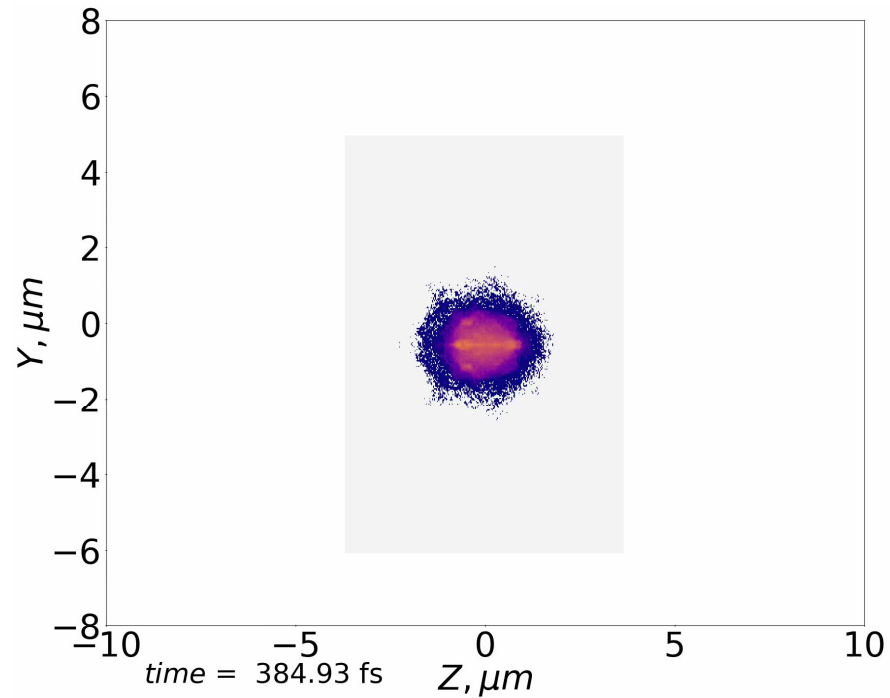
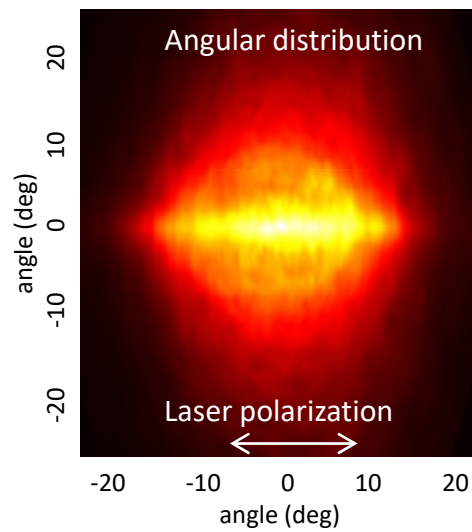
Electron spot



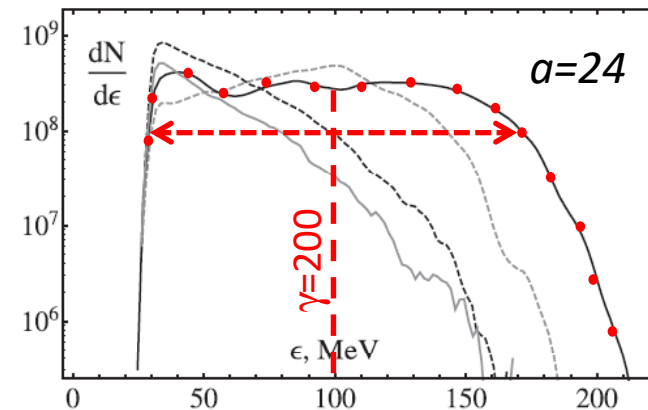
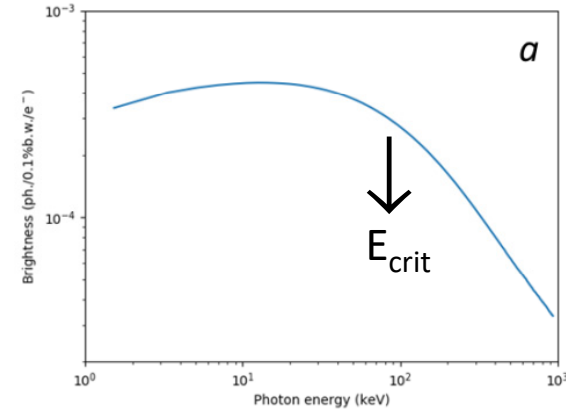
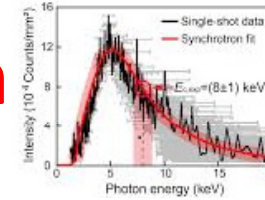
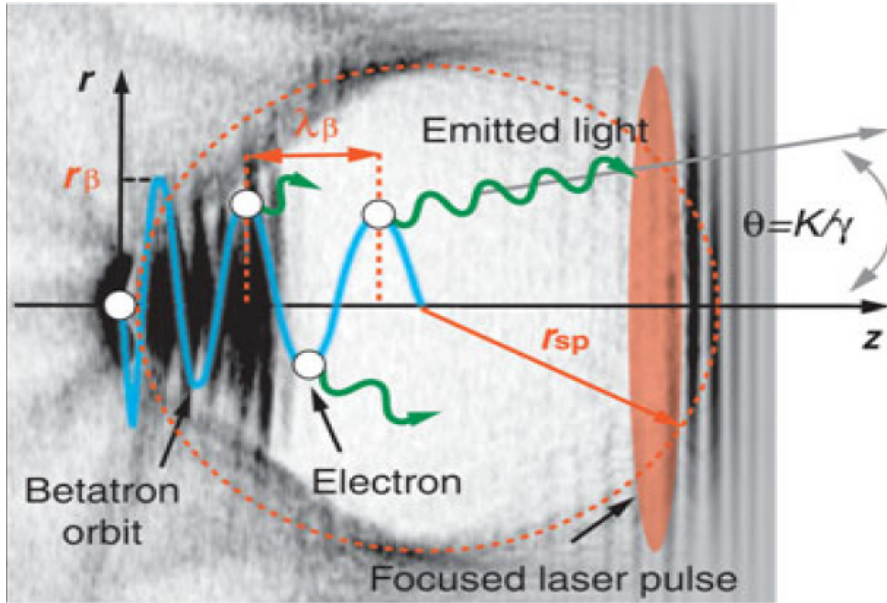
$$\Delta z \approx 0.16\lambda a_0$$

$$T \approx 0.25\lambda a_0^2/c$$

electron divergence is approximately 50 mrad, that corresponds to the emittance of about $0.1 \text{ rad} \times \mu\text{m}$



Hard x-ray betatron radiation



$$E_{\text{crit}} = \hbar\omega_{\text{crit}} \simeq 5 \times 10^{-24} \gamma^2 (n_e / \text{cm}^{-3}) (r_\beta / \mu\text{m}) \text{keV}.$$

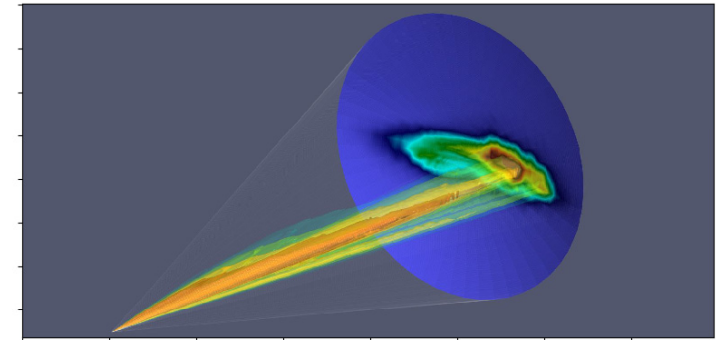
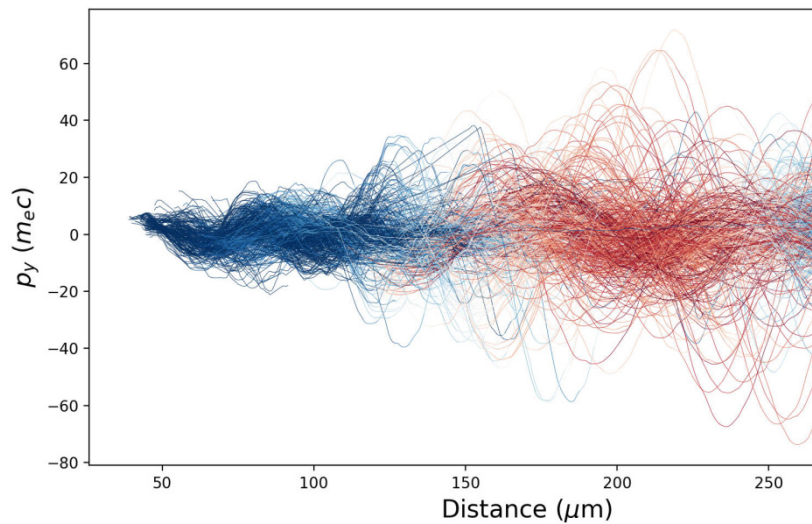
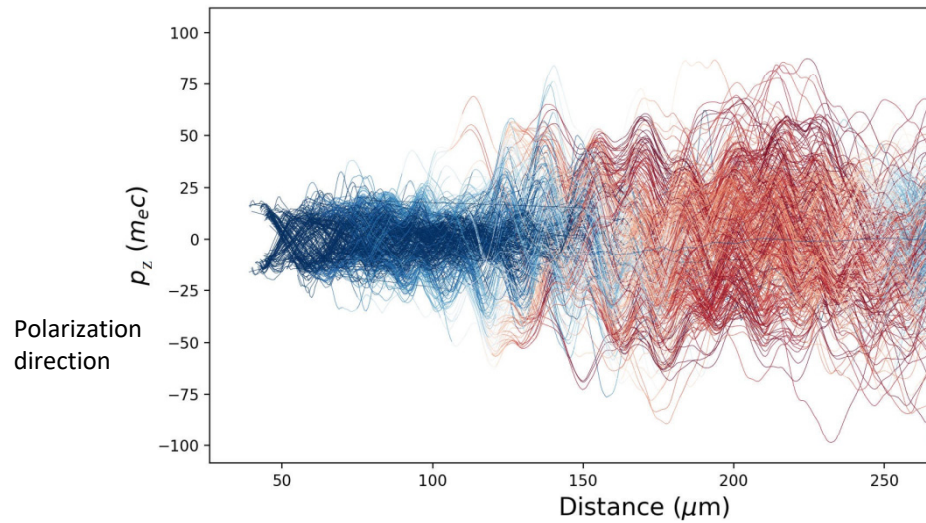
$$\gamma = 200, n_e = 20^{20} \text{ cm}^{-3}, r_\beta = 5 \mu\text{m}$$

$$E_{\text{crit}} = 100 \text{ keV}$$

Energy spectra of high-energy (>30 MeV) electrons leaving optimum thickness targets of different densities $1n_c$ (gray curve), $0.75n_c$ (black dashed curve), $0.1n_c$ (black curve), and $0.05n_c$ (gray dashed curve).

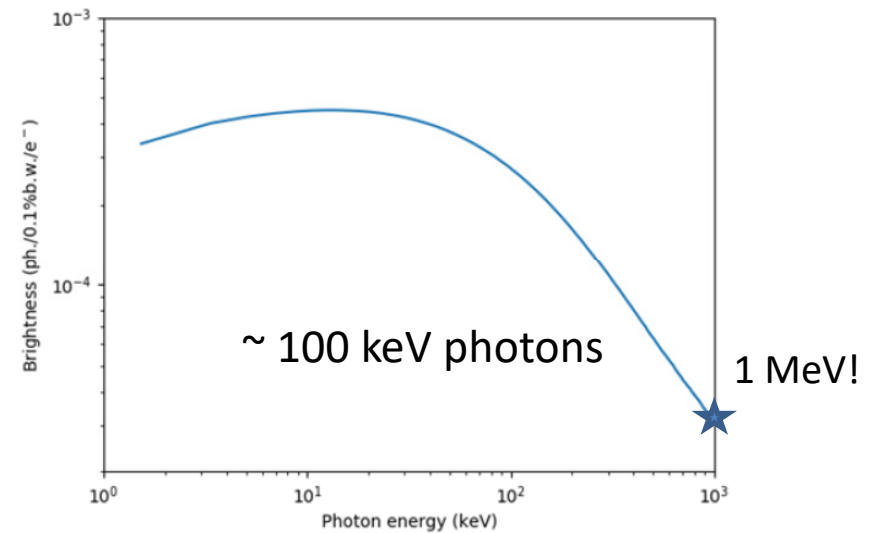
Betatron emission I

Randomly chosen $(1-1.5) \times 10^4$ trajectories of high-energy electrons
+ Lienard-Wiechert vector potential approach



$$a_0 = 24 \rightarrow \simeq 8 \times 10^{20} \text{ W/cm}^2$$

130 TW

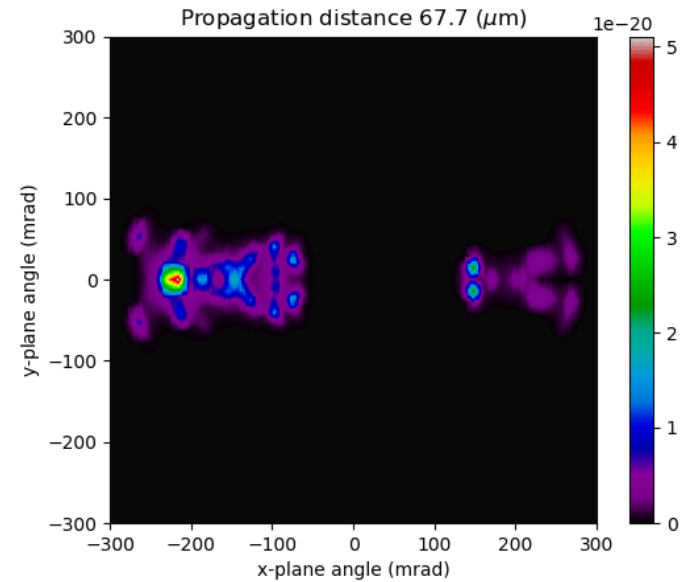
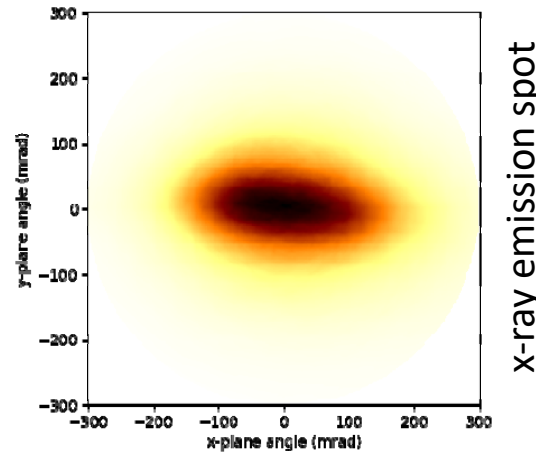
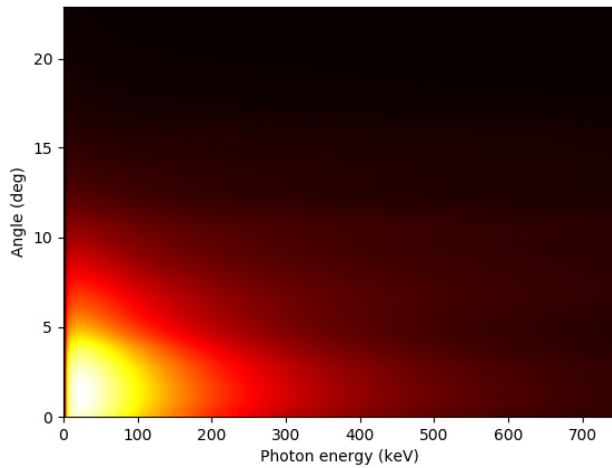


Betatron emission II

peak brightness, > 100keV
 10^{21} ph/0.1%b.w./mrad²/mm²/s

polarization degree, $P \simeq 1/3$.

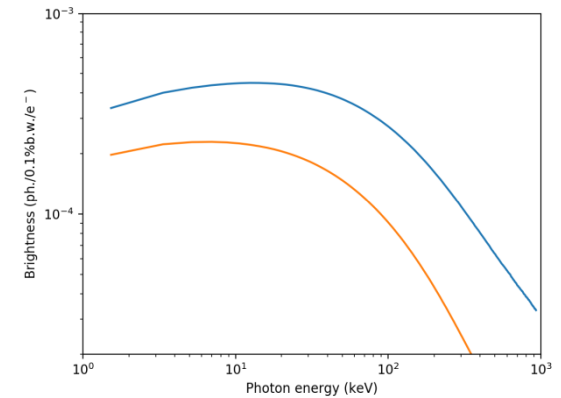
X-ray distribution



Spectral-angular distribution of the photons (from the electrons with energy > 30 MeV) in a far-eld zone.

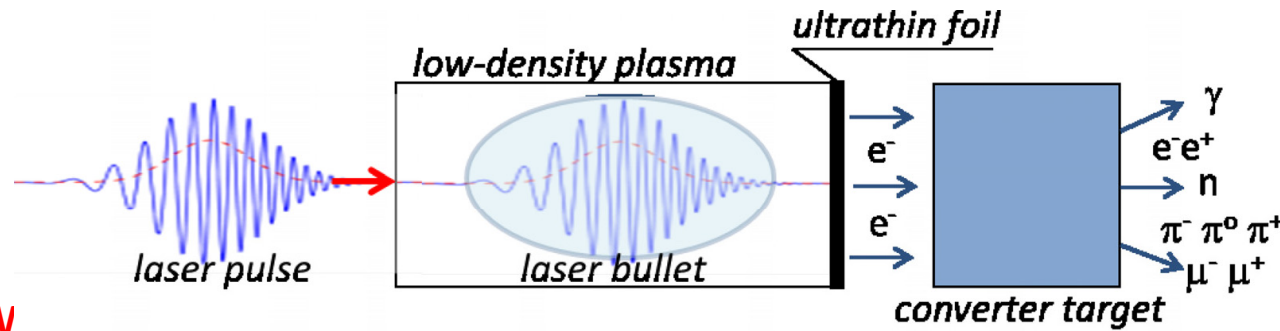
5×10^{10} photons > 10 keV
 Photon energy ~ 0.5 mJ

To study magnetic materials
 To study local electronic structure



→ Strongly polarized x-rays

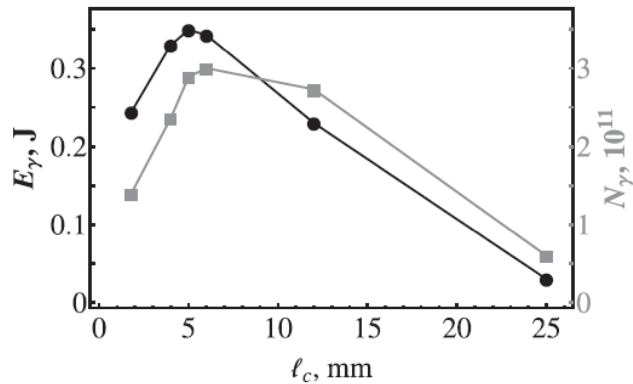
Electron conversion to gammas, e^-e^+ , photonuclear products



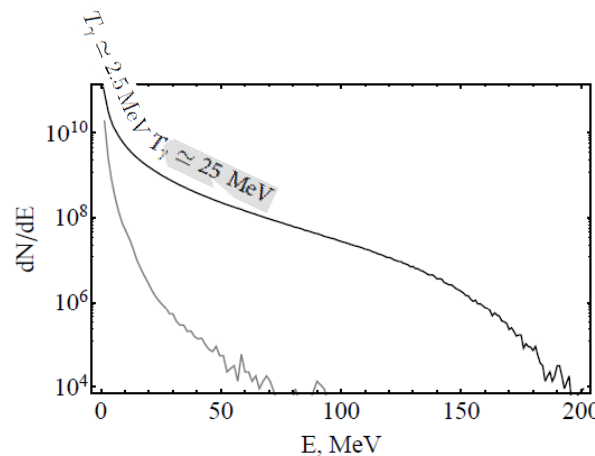
130 TW.

$8 \times 10^{20} \text{ W/cm}^2$, $\lambda = 1 \mu\text{m}$, 30fs, $d = 4 \mu\text{m}$, $n_e = 0.1 n_c$, $Q = 7 \text{ nC}$

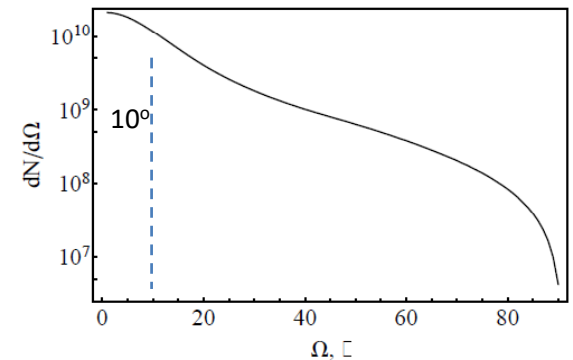
Converter			
Pt194	Z = 78	N = 194	32.967 %
Pt195	Z = 78	N = 195	33.832 %
Pt196	Z = 78	N = 196	25.242 %
Pt198	Z = 78	N = 198	7.163 %



Total yield (left) and energy (right) of gamma rays vs the thickness l_c of the Pt converter target for the laser-plasma parameters $P = 130 \text{ TW}$, $R_L = 2\lambda$, and $n_e = 0.1 n_c$ corresponding to an electron bunch with $Q \approx 7 \text{ nC}$ and an average energy of 100 MeV.



The energy spectra of gamma rays generated in the forward (black) and backward (gray) directions (left panel) and angular distribution of gamma-rays generated in the forward direction (right panel) from a 6 mm thick Pt target for the laser-plasma parameters $P = 130 \text{ TW}$, $R_L = 2\lambda$, and $n_e = 0.1 n_c$ corresponding to an electron bunch with $Q \approx 7 \text{ nC}$ and an average energy of 100 MeV.

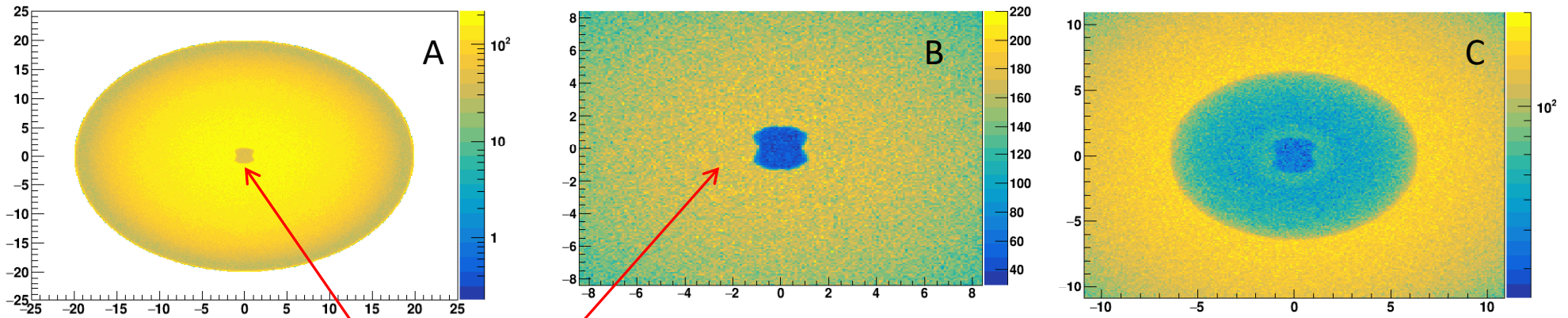


3×10^{11} photons, $\sim 0.35 \text{ J}$ $\sim 8\%$ laser-to-gamma conversion efficiency,

10 MeV gamma brightness $\sim 10^{19} \text{ s}^{-1} \text{ mrad}^{-2} \text{ mm}^{-2} (0.1\% \text{ BW})^{-1}$

γ spot size and duration
60 μm , 300 fs

Single shot deep gamma-radiography (130 TW, 30 fs)

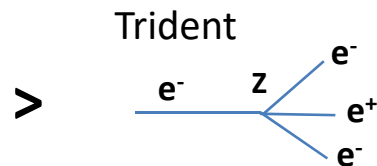
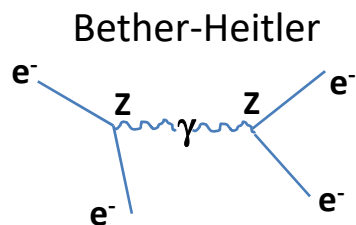


A crumpled platinum tube 5 meters from the converter, surrounded by a 3 cm iron shell (Fig. 2A, B). Fig. 2C: the platinum tube is additionally surrounded by a 10 cm aluminum shell. Detector dimensions in centimeters. Detector of the typical type used in PET imaging with a pixel size of (1-3) mm².

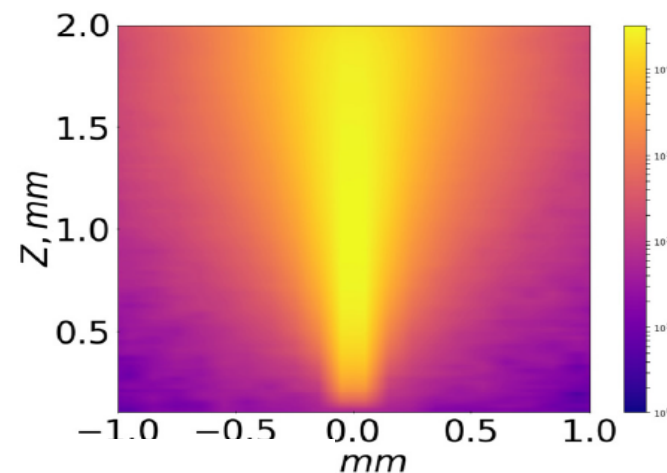
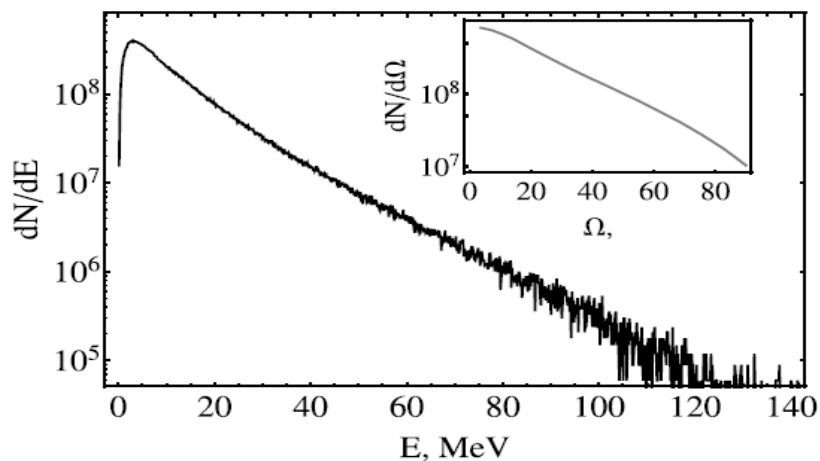


Mobile inspection system for special nuclear materials

Positron generation



$$n_{e^+} = 2 \times 10^{12} \text{ cm}^{-3}$$

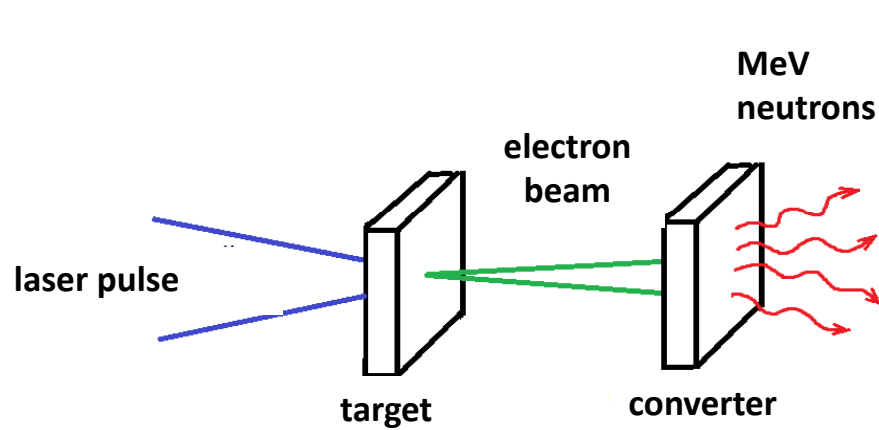


Energy spectrum of positrons generated from a 6 mm Pt target (left panel) and positron flux in a 1.8 mm Pt target (right panel) for the laser-plasma parameters $P = 130 \text{ TW}$, $R_L = 2\lambda$, and $n_e = 0.1n_c$ corresponding to an electron bunch with $Q \simeq 7 \text{ nC}$ and an average energy of 100 MeV. The inset in the left panel shows the angular distribution of positrons generated from the 6 mm Pt target.

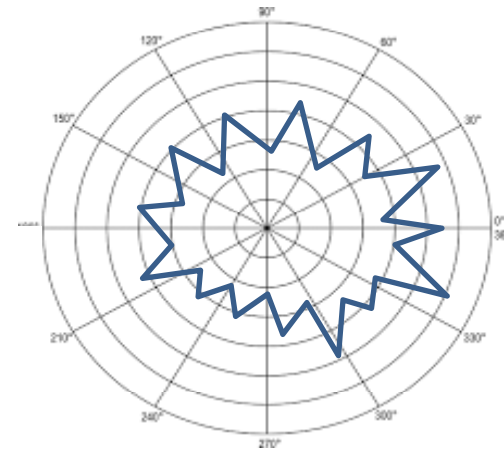
$$N_{e^+} = 9 \times 10^9 \quad \text{6 mm thick Pt target} \quad N_e \gg N_{e^+}$$

The positron jet angular spread increases from $\sim 20^\circ$ for a 1.8 mm Pt converter target to $\sim 35^\circ$ for a 6 mm target and $\sim 40^\circ$ for a 12 mm target.

Electron conversion to neutron emission



$8 \times 10^{20} \text{ W/cm}^2$, $\lambda = 1 \mu\text{m}$, 30 fs ,
 $d = 4 \mu\text{m}$, $n_e = 0.1 n_c$, $Q = 7 nC$



6.5×10^{-3} neutrons/electron

nearly isotropic
neutron
distribution

$2 \times 10^8 \text{ n}^\circ$

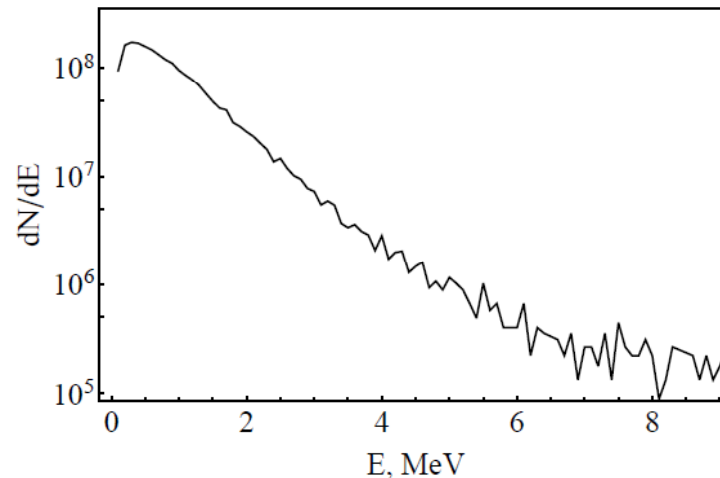
dominance

(γ, n) , $(\gamma, 2n)$, (γ, np) , $(\gamma, 3n)$,

highrep laser is
required (kHz)

$K_n \sim 10^{-5}$

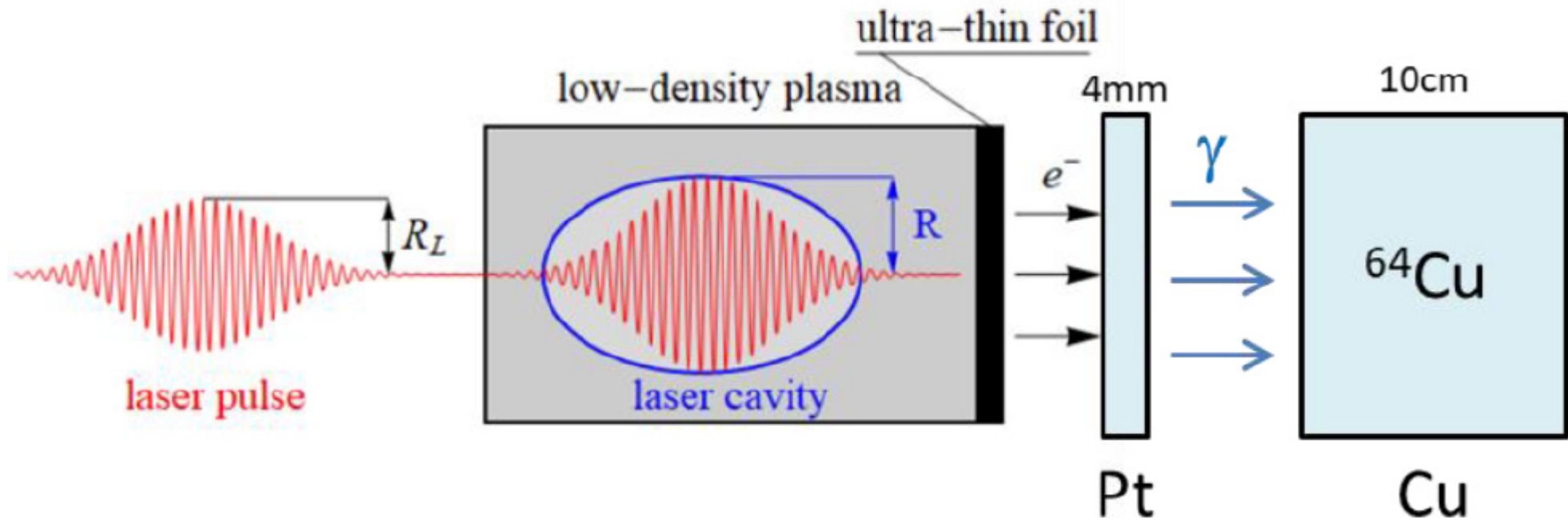
giant dipole resonance (GDR), 10 – 20 MeV



Energy spectrum of neutrons generated from a 12 mm thick Pt target outside the target the forward and backward directions (at a 108° angle in both cases)

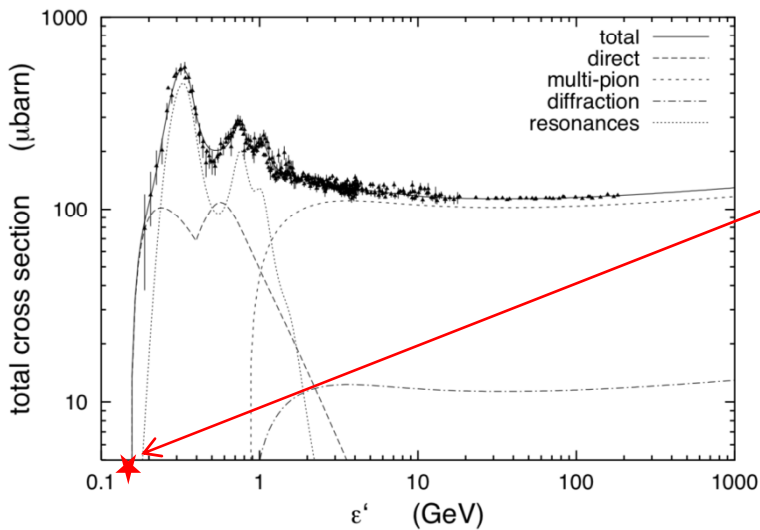
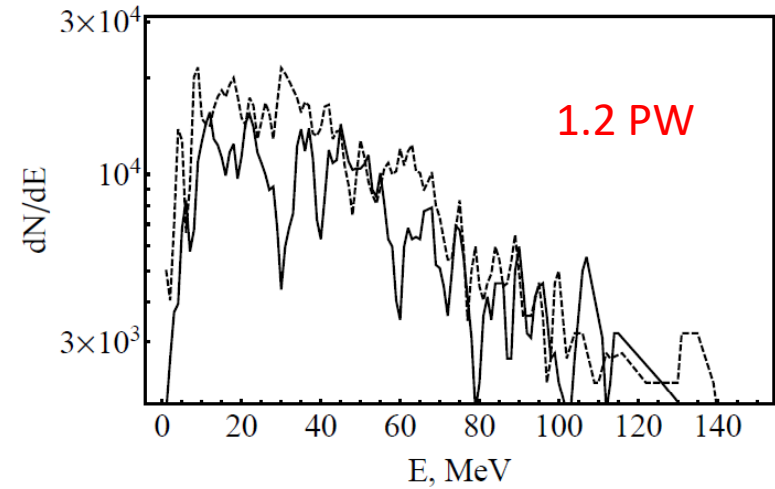
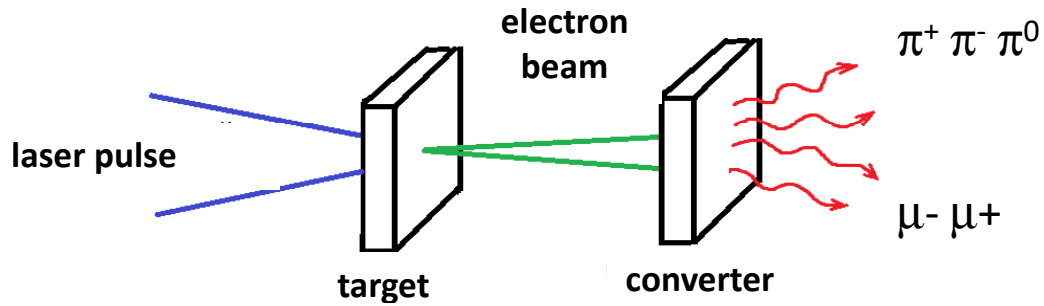
In general, photonuclear cross-section is smaller than typical nuclear cross sections due to the electromagnetic nature of interaction. However, at the resonance energy it is comparable on the order of magnitude with the geometrical nuclear cross section that well compensate a weakness of electromagnetic interaction.

PET isotope production (^{64}Cu)



Numerical simulation scheme for isotope ^{64}Cu production for PET. Simulation parameters: $P=130$ TW, focal spot size = $6\mu\text{m}$, pulse duration = 30 fs, plasma electron density = $0.1n_c$. **The yield of the isotope ^{64}Cu is 3×10^8** , that is unattainable for the reaction $^{64}\text{Ni} + p$ from a perfectly optimized scheme with an ultrathin solid dense foil (A.V.Brantov et al., Phys. Rev. AB 18, 021301 (2015)).

Photoproduction of mesons



130 TW

$$\pi^+ \approx \pi^0 \Rightarrow 160, \pi^- \Rightarrow 210$$

$$\Sigma = 530$$

Cf. W. Schumaker et al.,
New J. Phys. **20**, 073008, 2018

1.2 PW

$$\pi^+ \approx \pi^0 \Rightarrow 7 \times 10^5, \pi^- \Rightarrow 1 \times 10^6$$

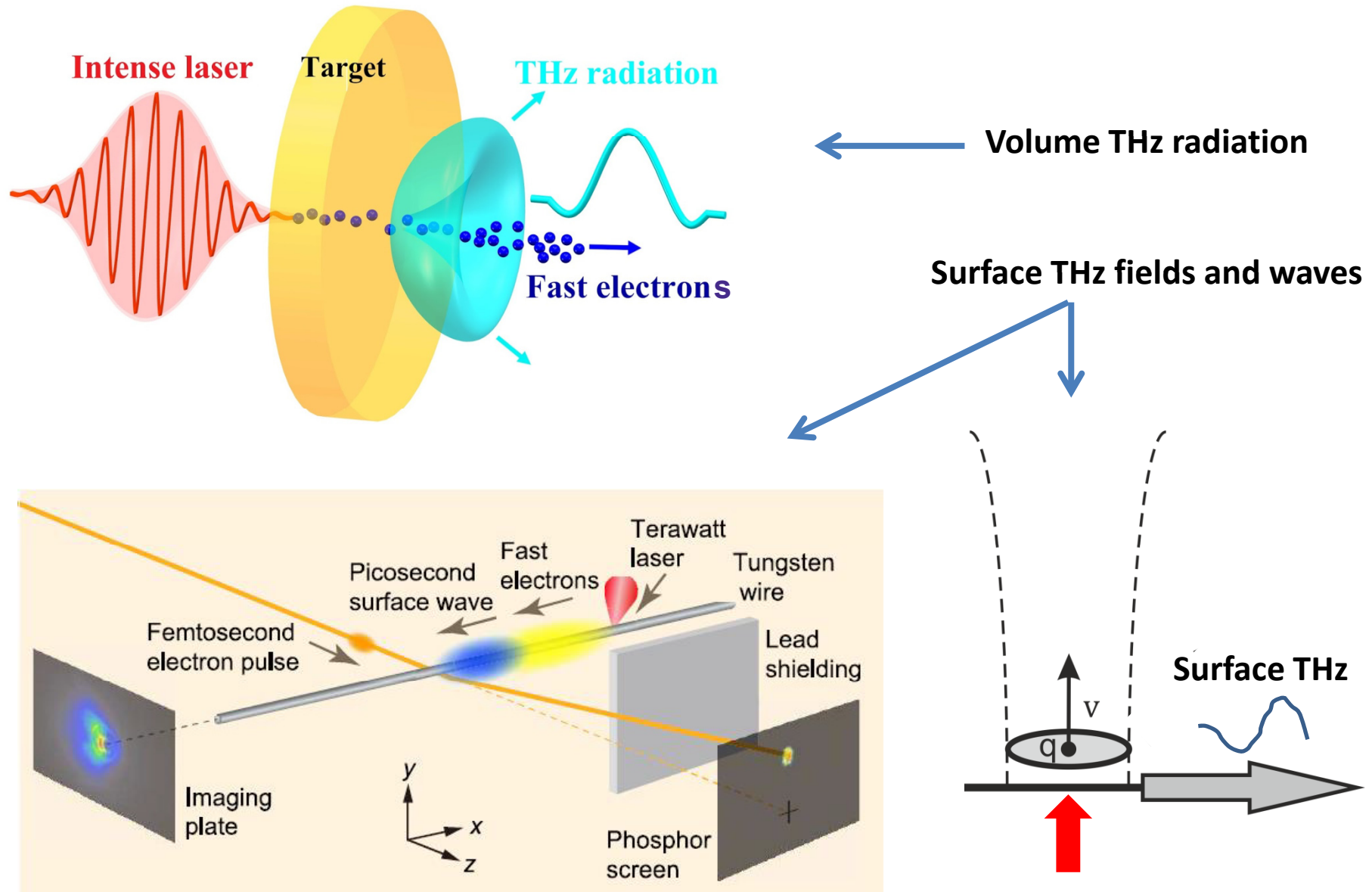
unstable

$$\Sigma = 2.4 \times 10^6$$

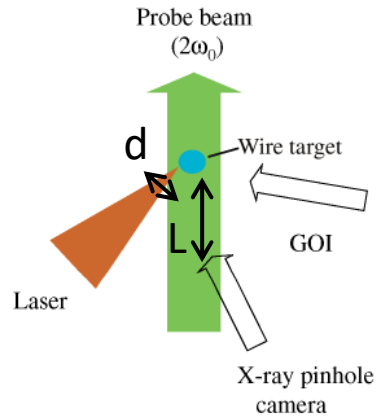
Spectra of photonuclear
generated π^+ (solid line) and
 π^- (dashed line) pions

$\mu^- \mu^+$ pairs
were detected
only from several PW pulse

Laser-triggered extreme THz fields and waves



Mysterious waves. π - wave.

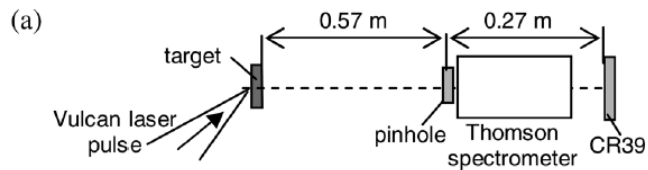


F. N. Beg et al.,
PRL 92, 095001 (2004)

VULCAN up to 5×10^{19} W/cm²

L - several hundred microns
d ~ 15 μ m

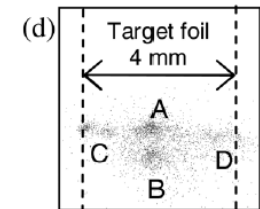
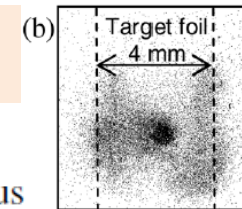
induced MA-current
along a wire !



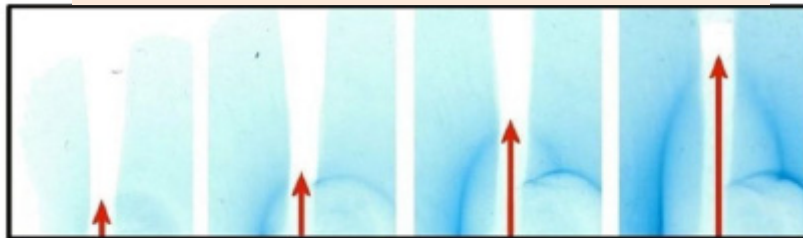
Ion
acceleration

P. McKenna et al.,
PRL 98, 145001 (2007)

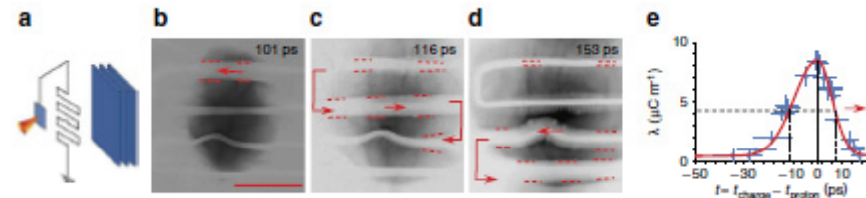
measurement of large electric fields (~ 0.1 TV/m) millimeters from the laser focus



K. Quinn et al., Phys. Rev. Lett. 102 194801 (2009)



S. Kar et al., Nat. Commun. 7, 10792 (2016)

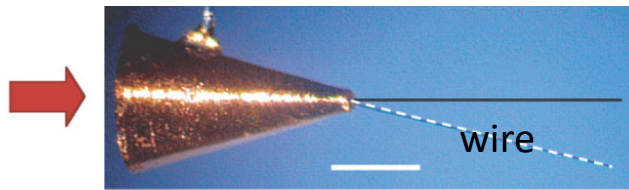


Tokita, S. et al., PRL 106, 255001 (2011);
Sci. Rep. 5, 8268 (2015).

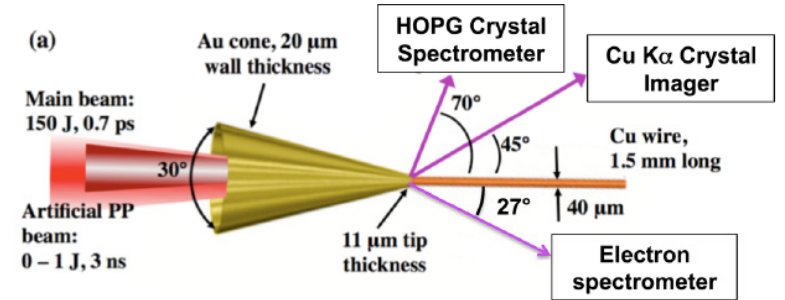
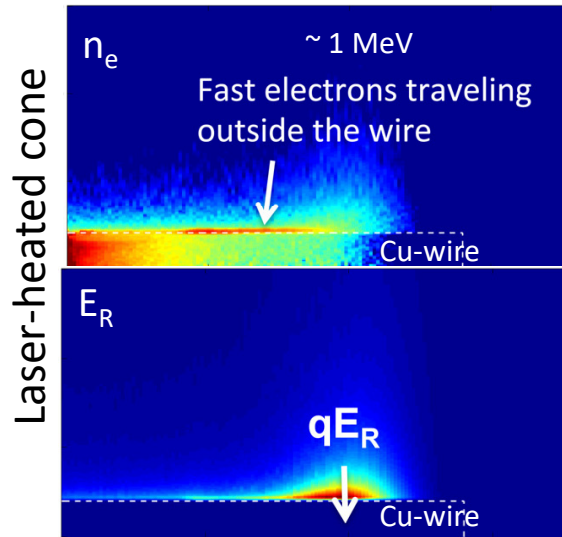
H. Nakajima et al.,
PRL 110, 155001 (2013)

R. Pompili et al.,
Sci. Rep. 8, 3243 (2018)

Relativistic electron beam guiding along a thin wire



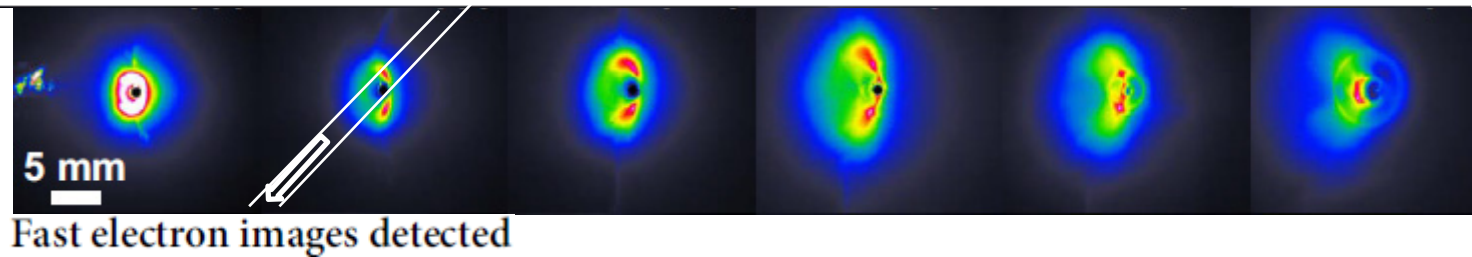
R. Kodama et al.,
Nature 432, 7020 (2004)
M. Borghesi et al.,
CLF Ann. Rep. 2006, p.13, Vulcan



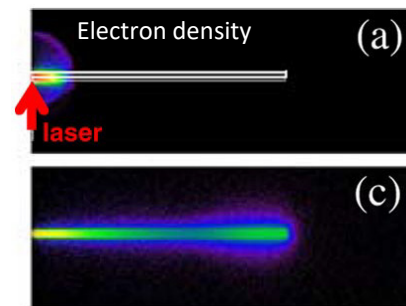
TITAN cone-wire experimental setup (LLNL, 2012)

S. Tokita et al.,
Sci. Rep. 5, 8268 (2015)

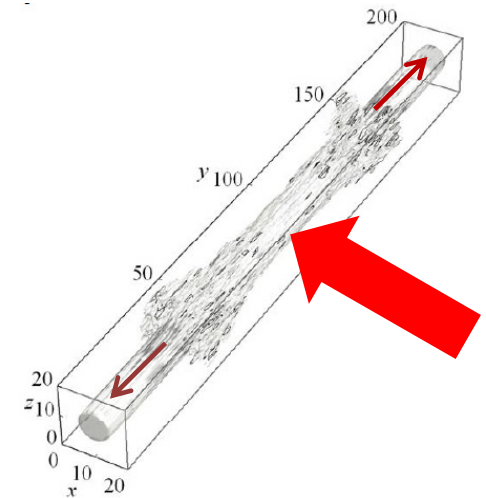
$d = 12$ mm 24 mm 36 mm 64 mm 74 mm 114 mm



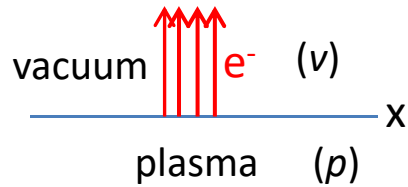
P. McKenna et al.,
PRL 98, 145001 (2007)



A.V.Brantov et al.,
EPJ Web Conf.
195, 03002 (2018)



Theory of ultrafast target charging



The full set of Maxwell equations with external current, $\mathbf{j} = en_e \mathbf{v}$

$$\frac{\partial^2 E_x^{p,v}}{\partial x^2} - k_{p,v}^2 E_x^{p,v} = \frac{4\pi e}{\epsilon} \frac{\partial \epsilon n_{\omega,k}^e}{\partial x} - \frac{4\pi e i \omega v}{c^2} n_{\omega,k}^e \quad n_e = n^e(x - vt, \mathbf{r}_\perp)$$

$$\mathbf{k} \perp \mathbf{x}, \mathbf{v} = (v, 0, 0), k_v = \sqrt{\mathbf{k}^2 - \omega^2/c^2}, k_p = \sqrt{\mathbf{k}^2 - \epsilon \omega^2/c^2} \quad n_{\omega,k}^e = n^e i \omega x / v$$

$$E_x^v = -\frac{4\pi e n k v}{v^2 k_v^2 + \omega^2} \left(\frac{i\omega}{k v} \left(1 - \frac{v^2}{c^2} \right) e^{i \frac{\omega x}{v}} + \frac{k(\epsilon - 1)(v k_p + i\omega(1 - v^2/c^2))}{(k_p + \epsilon k_v)(v k_p + i\omega)} e^{-k_v x} \right)$$

$$E_x^p = -\frac{4\pi e n k v}{\epsilon(v^2 k_p^2 + \omega^2)} \left(\frac{i\omega}{k v} \left(1 - \epsilon \frac{v^2}{c^2} \right) e^{i \frac{\omega x}{v}} + \frac{k(\epsilon - 1)(v k_v - i\omega(1 - \epsilon v^2/c^2))}{(k_p + \epsilon k_v)(v k_v - i\omega)} e^{k_p x} \right)$$

High-conductivity, $|\epsilon| \rightarrow \infty \quad E_x^p = 0$

The pole: $k_p + \epsilon k_v = 0, \quad k_0 \simeq \pm \omega/c(1 - 1/(2\epsilon))$

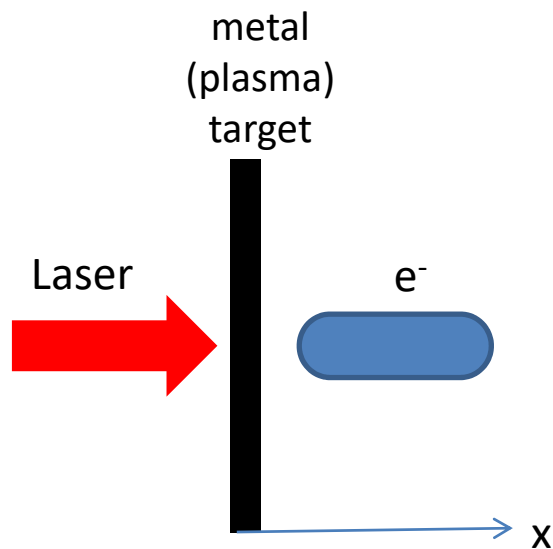
$$E_x^{sv} = - \int \frac{d\omega 2i e n v \omega}{c^2 \sqrt{-\epsilon}} e^{-i\omega(t \pm \frac{z}{c})} e^{-i \frac{\omega}{2\epsilon c} |z|} e^{-\frac{\omega x}{c\sqrt{-\epsilon}}}$$

2D geometry, (x,z), filiform (along y) point charge

$$E_{x0}^v = \begin{cases} -\frac{4\lambda}{\sqrt{c^2 t^2 - z^2}} \frac{c v t^2 \gamma^2}{z^2 + v^2 t^2 \gamma^2}, & z^2 < c^2 t^2 \\ 0, & z^2 > c^2 t^2 \end{cases}$$

λ is the linear charge density

Polarization field



$v < c$

point charge

q

E_x

растекание заряда

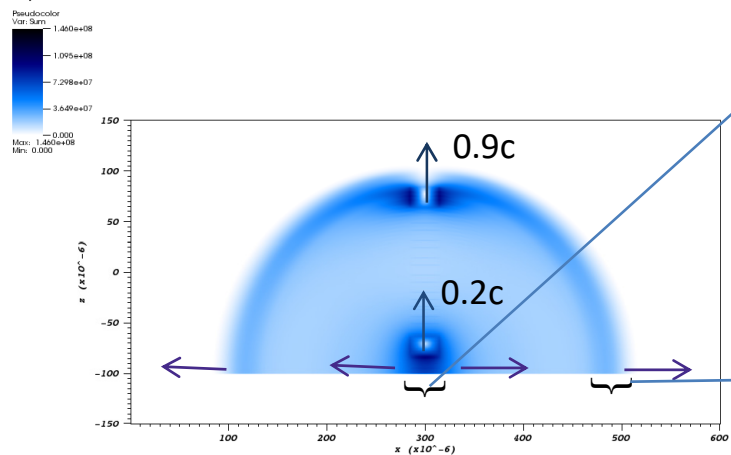
$v = c (\gamma \gg 1)$

q

E_x

волна заряда

DB: Main_YeeElecField_71.h5
Cycle: 700 Time: 7e-13



user: 70-kas
Mon Feb 10 15:23:02 2020

Ultrafast target charging due to polarization triggered by laser-accelerated electron bunches

The same physics holds for a finite-sized electron charge and is described analytically for $|\epsilon| \gg 1$ and $\gamma \gg 1$ or $\gamma \ll 1$.

$$E_x^v = -\frac{4\pi en e^{-k_v x}}{ck_v}, E_x^p = \frac{4\pi en}{\epsilon} \left[\frac{e^{i\frac{\omega x}{c}} - e^{k_p x}}{i\omega} - \frac{e^{k_p x}}{ck_p} \right]$$

$$B_y^v = -\frac{4\pi en}{ck} \left(\frac{\omega}{ck_v} e^{-k_v x} - i e^{i\frac{\omega x}{c}} \right),$$

$$B_y^p = -\frac{4\pi en}{ck} \left(\frac{\omega}{ck_p} e^{k_p x} - i e^{k_p x} \right),$$

$$E_z^v = \frac{4\pi i en}{ck} \left(e^{-k_v x} \left[1 + \frac{\omega}{ck_p} \left(\frac{\omega}{ck_v} - i \right) \right] - e^{i\frac{\omega x}{c}} \right)$$

$$E_z^p = \frac{4\pi i \omega en}{c^2 k k_p} \left(\frac{\omega}{ck_v} - i \right) e^{k_p x}.$$

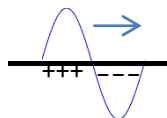
$$\epsilon = 1 - \omega_p^2/\omega^2 \simeq -\omega_p^2/\omega^2 \quad \omega_* \simeq \min\{\tau^{-1}; c/L\}$$

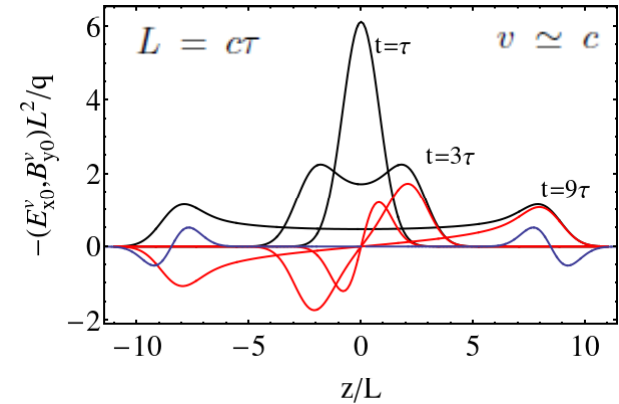
$$en^e = \lambda \theta(t) (\theta(vt - x) - \theta(vt - c\tau - x)) \exp(-z^2/L^2) / (Lv\tau\sqrt{\pi})$$

$\sim 100pC/\mu m$ escaping from the spot with $L \sim 5\mu m$ can generate surface electric field up to TV/m.

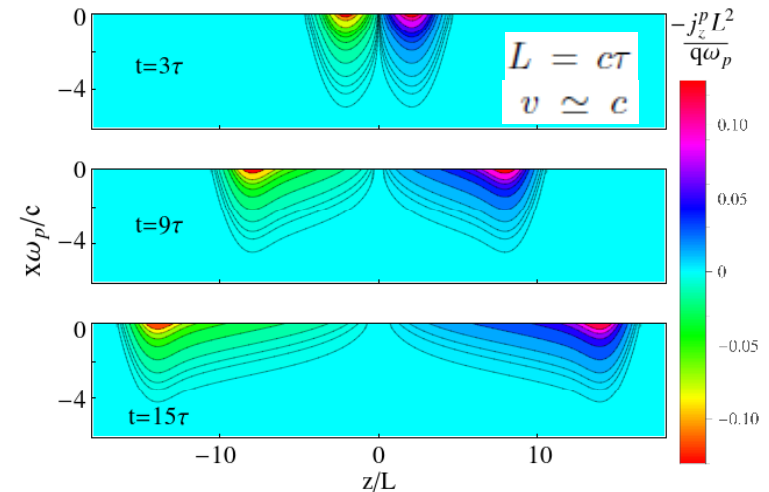
$$E_x^{sv} = \frac{4\sqrt{\pi}\lambda}{\omega_p \tau L} \left(e^{-\frac{(ct \mp z)^2}{L^2}} - e^{-\frac{(ct - c\tau \mp z)^2}{L^2}} \right)$$

- surface wave



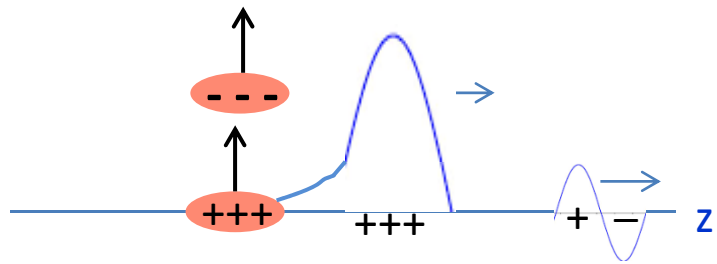


$$j_z^p = \frac{i\lambda\omega_p}{2c\tau} \int \frac{dk}{\pi k} [J_0(ck(t-\tau)) - J_0(ckt)] e^{-\frac{k^2 L^2}{4}} e^{ikz + \frac{c\tau}{\omega_p}}$$

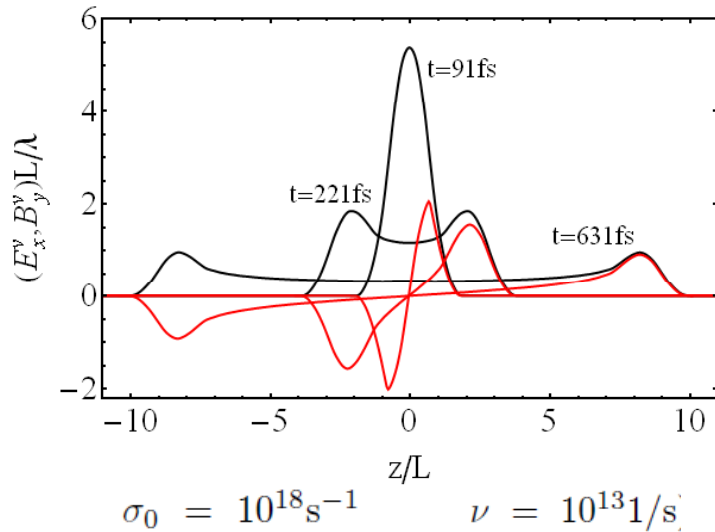


Simulations of the polarization charging

1 FDTD-simulations, $Q_{\text{tot}} = 0$

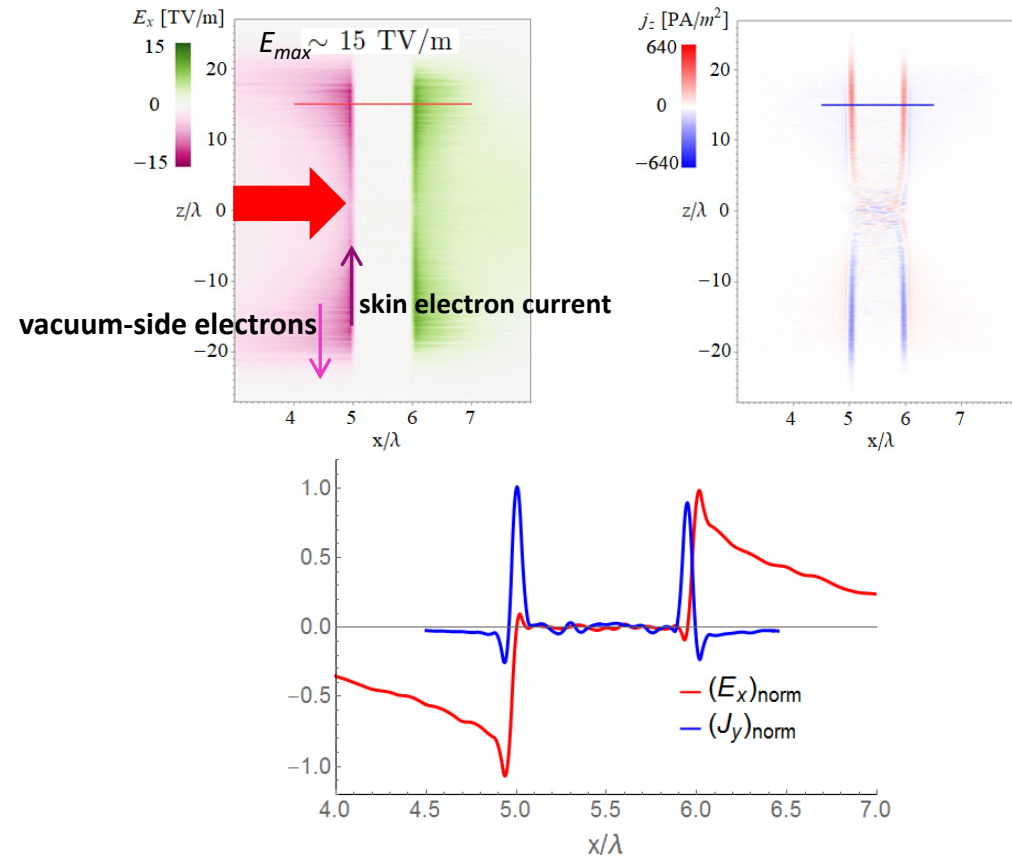


Drude model, $\epsilon = 1 + 4\pi i\sigma(\omega)/\omega$
 $\sigma = \sigma_0/(1 - i\omega/\nu)$

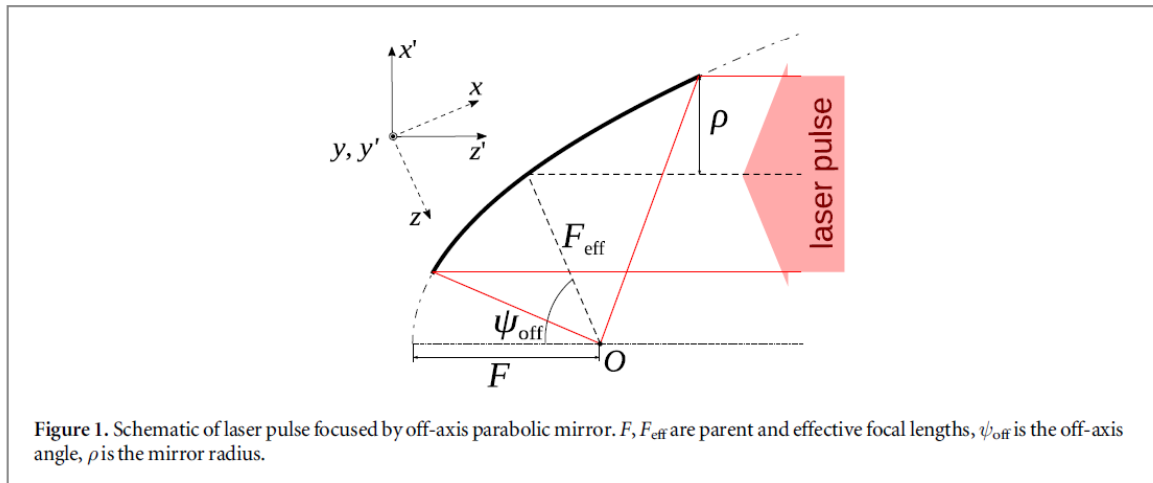


2 2D PIC-simulations

multi-GeV/m field at the distance $\sim 1\text{cm}$



Extreme light diagnostics by ponderomotive acceleration of protons from rarified gas



O. Vais et al., New J. Phys. 22, 023003 (2020).

$$1) \quad \frac{d\gamma \mathbf{v}}{dt} = \frac{q}{m} \left(\mathbf{E} + \frac{[\mathbf{v} \times \mathbf{B}]}{c} \right), \quad \frac{d\mathbf{R}}{dt} = \mathbf{v}$$

$$2) \quad \gamma \simeq 1 \quad a_{0p} = \frac{a_0}{1840} \quad a_{0p} \ll 1$$

$$\vec{F}_p = -\frac{q^2}{4m\omega^2} \nabla |\vec{E}|^2$$

Focal laser field at the diffraction limit, $D_F \sim \lambda$

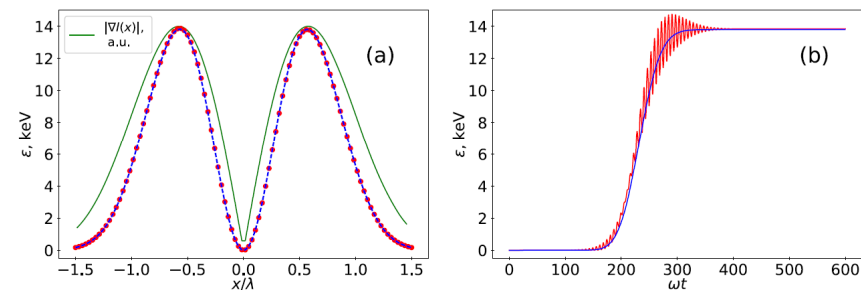
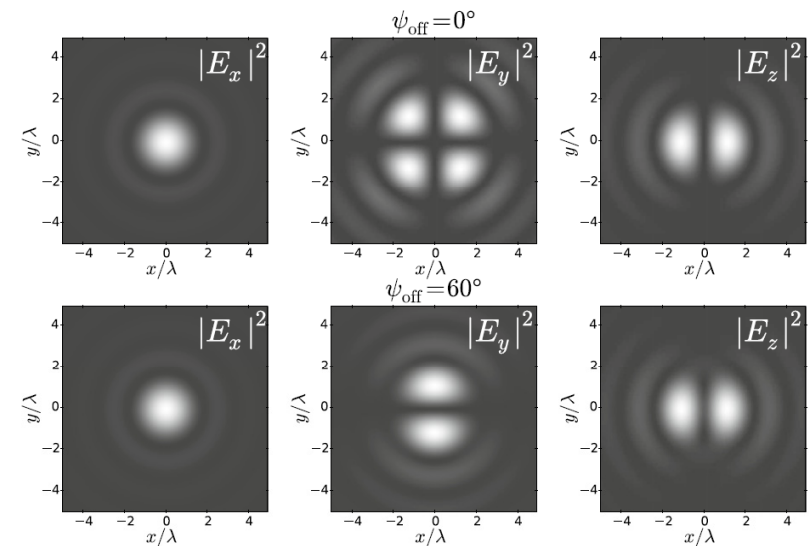
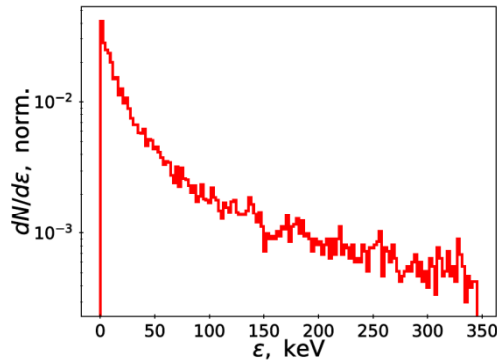


Figure 2. Comparison of results obtained by Lorentz force (red color) and ponderomotive force (blue color): (a) final energy as a function of initial proton position along x -axis ($y = 0, z = 0$) and the absolute value of intensity gradient of Gaussian laser beam (green line), (b) average energy (from the ponderomotive approximation) and its moving average (from Lorentz approach) as a function of time. Numerical calculations were performed for a Gaussian laser pulse with peak intensity $I_p = 10^{22} \text{ W cm}^{-2}$ and $\tau_{\text{FWHM}} = 36 \text{ fs}$, focused to a spot of size $D_F = 1.32\lambda$.

Diagnostics: intensity, focusing sharpness



ϑ -integrated spectral distributions of protons accelerated by a Gaussian laser pulse with duration $\tau=36$ fs and peak intensity $I=5 \times 10^{22} \text{ W cm}^{-2}$, focused by an off-axis parabolic mirror ($\rho = 5.08$ cm, $\psi_{\text{off}} = 90^\circ$) to a focal spot size $D_F=1.3\lambda$.

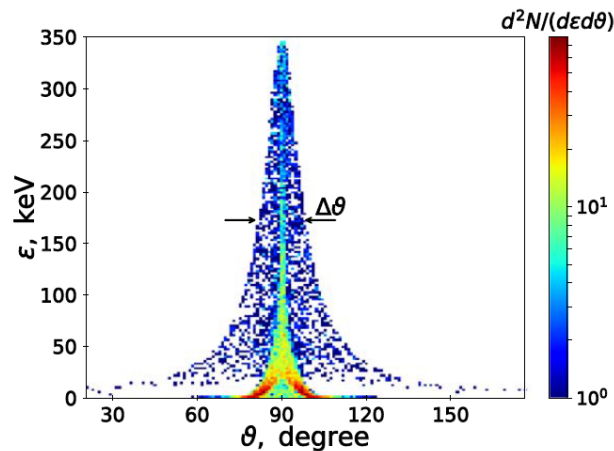
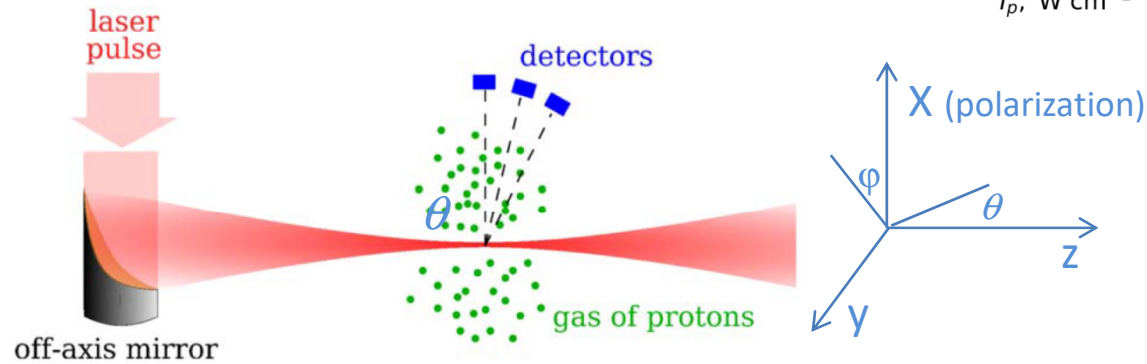
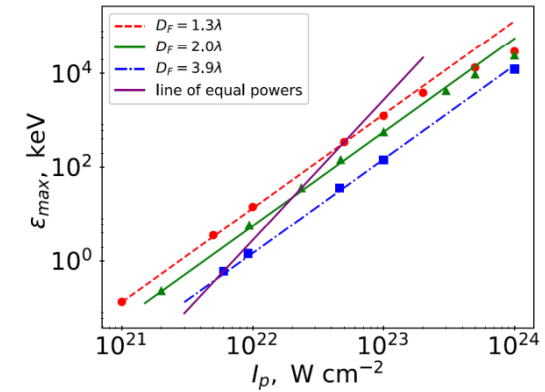
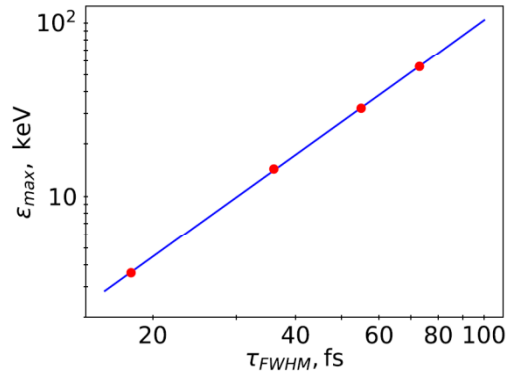


Table 1. Numerically calculated angular width of proton spectra for different values of the focal spot size for the Gaussian laser pulse.

$f\#$	D_F	z_R	$\Delta\vartheta$, deg.	$\tan(\Delta\vartheta/2)$	$\tan(\Delta\vartheta/2)/(D_F/z_R)$
1	1.3λ	7.8λ	15.4	0.14	0.84
1.5	2.0λ	18λ	9.8	0.086	0.77
3	3.9λ	73.6λ	4.95	0.043	0.81

Diagnostics: pulse duration, spatial focal inhomogeneity



The cutoff energies as a function of the pulse duration τ_{FWHM} of the Gaussian laser pulse with $I=10^{22} \text{ W cm}^{-2}$ and $D_F=1.32\lambda$. Dots show results of numerical calculations, line is a result of the fitting.

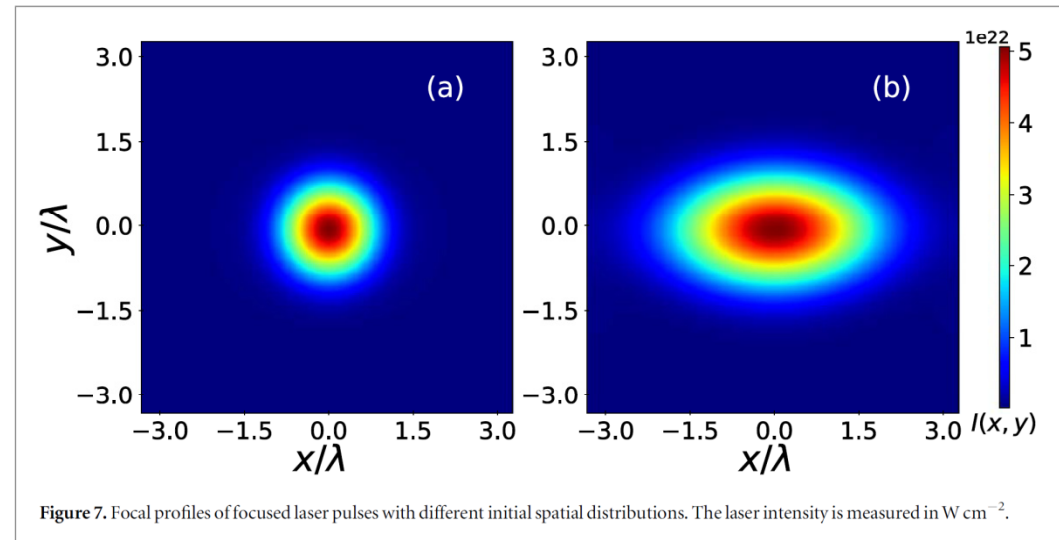


Figure 7. Focal profiles of focused laser pulses with different initial spatial distributions. The laser intensity is measured in W cm^{-2} .

$$\exp(-(x'^2 + y'^2)/w_0^2)$$

$$\exp(-(x'^2 + y'^2)/w_0^2) \Theta(x')$$

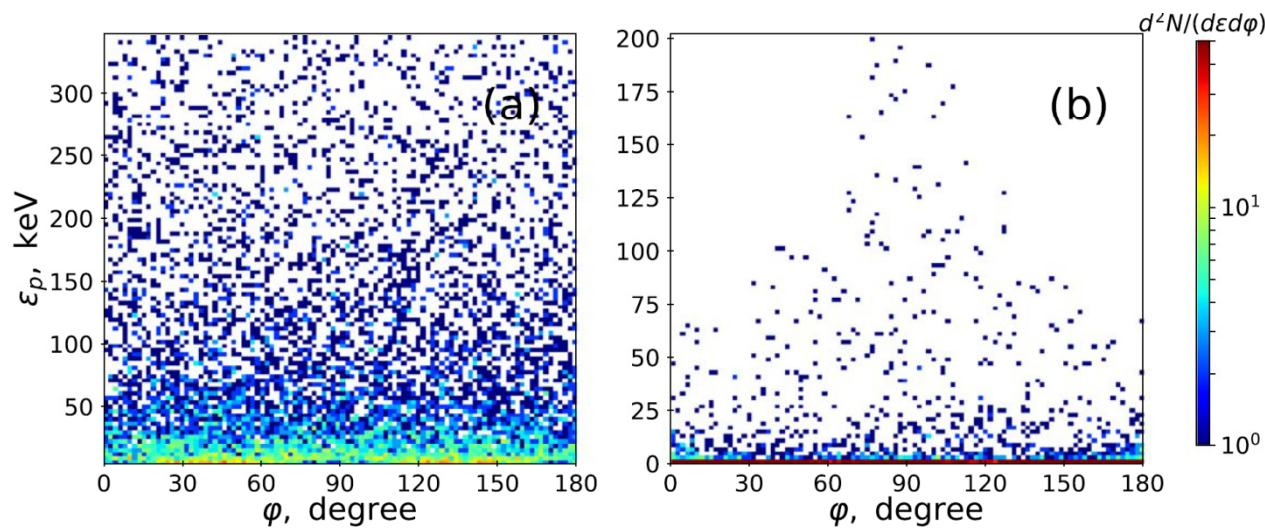


Figure 8. φ -integrated spectral distributions of protons accelerated by axial symmetric (a) and anisotropic (b) laser pulses, corresponding to the focal distributions shown in figures 7(a) and (b).

Practical
implementation

$$N_V > 10^4$$

$$n_H < 10^{16} \text{ cm}^{-3}$$

chevron type MCP detectors
and/or
nuclear track detectors CR-39

Conclusions

- Electron acceleration in self-trapping regime from low density targets provides maximum total electron charge for relativistic pulses.
- Self-trapping regime makes it useful for production of gammas and photonuclear particles from converter target.
- Betatron emission demonstrates the record yield and photon energy (up to MeV) from self-trapping regime.
- Other nuclear applications can be of interest (fission, transmutation).
- The physics of ultrafast target charging in a wave form due to polarization triggered by laser-accelerated electrons is well clarified and founded.
- Weaker, but still intense, field pulse can propagate along surface (wire) in the form of surface (Sommerfeld) wave for a long distance.
- Innovative diagnostics of ultra-intense laser pulses through ion acceleration is proposed.

Thank
you